



RF Reflectometry of Single-Electron Circuits

Part A: Lumped element model of a co-axial transmission line (2.0 points)

A.1 (0.2 pt)

$v =$

A.2 (0.2 pt)

$E(r) =$

A.3 (0.3 pt)

$C_x =$

A.4 (0.3 pt)

$L_x =$

A.5 (1.0 pt)

i.

ii. $b/a =$

Part B: Hypothetical transmission line with return along a grounded plane (1.0 points)

B.1 (1.0 pt)

$Z_0 =$

Part C: Basics of RF reflectometry (1.2 points)

C.1 (1.0 pt)

$\Gamma =$

C.2 (0.2 pt)

Part D: The single electron transistor (points 3.3)

D.1 (1.5 pt)

i. $\varphi_n =$

ii. $\Delta E_n =$

**D.2** (0.5 pt) $E_c =$ **D.3** (0.5 pt)**D.4** (0.8 pt)i. $\tau =$

ii.

Part E: RF reflectometry to read out SET state (1.0 points)**E.1** (0.2 pt) $\Delta\Gamma =$ **E.2** (0.8 pt) $L_0 =$ $\Delta\Gamma =$ **Part F: Charge sensing with a single lead quantum dot (1.5 points)****F.1** (1.0 pt) $\omega_{\text{rf}} =$ $Z_C =$ **F.2** (0.5 pt)



X-ray jets from active galactic nuclei

Part A: 1D fluid model of a jet (3.8 points)

A.1 (0.3 pt)

$$n'(s) =$$

A.2 (0.2 pt)

$$F_p(s) =$$

A.3 (0.5 pt)

A.4 (0.6 pt)

A.5 (0.6 pt)

$$\frac{dP_1}{ds} =$$

A.6 (0.4 pt)

Expression for calculating $\dot{M}$:

$$\dot{M}_1 =$$

$$\dot{M}_2 =$$

A.7 (0.5 pt)

Expression:

$$\Pi =$$

Numerical:

$$\Pi =$$



A.8 (0.5 pt)

$$F_{\text{Pr}} =$$

A.9 (0.2 pt)

Relationship:

$$\% \text{ deviation} =$$

Part B: Gas of ultra relativistic electrons (2.2 points)

B.1 (0.2 pt)

B.2 (0.8 pt)

$$\frac{\Delta p_x}{\Delta t} =$$



B.3 (0.6 pt)



B.4 (0.6 pt)

Part C: Synchrotron emission (1.7 points)

C.1 (0.7 pt)

$$\Omega =$$

C.2 (0.5 pt)

$$\Delta t =$$

C.3 (0.3 pt)

$$\nu_{\text{chr}} =$$



C.4 (0.2 pt)

$\tau =$

Part D: Synchrotron emission from an AGN jet (2.3 points)

D.1 (0.4 pt)

$B =$

D.2 (1.0 pt)

$f(\epsilon) =$

D.3 (0.3 pt)

Synchrotron cooling will make the distribution:

☐ shallower, ☐ steeper, ☐ other

**D.4** (0.6 pt)

AGN	Knot	Likely cause of cooling	Question parts which support your conclusion
Cen A	AX1C	☐ synchrotron cooling ☐ adiabatic expansion ☐ neither	
Cen A	BX2	☐ synchrotron cooling ☐ adiabatic expansion ☐ neither	
M87	HST-1	☐ synchrotron cooling ☐ adiabatic expansion ☐ neither	
M87	Knot A	☐ synchrotron cooling ☐ adiabatic expansion ☐ neither	



Tippe top

Part A (10.0 points)

A.1 (1.0 pt)

$\mathbf{F}_{\text{ext}} =$

A.2 (0.8 pt)

$\tau_{\text{ext}} =$



A.3 (0.4 pt)

A.4 (0.8 pt)

$\omega =$

A.5 (1.0 pt)

$E_T =$

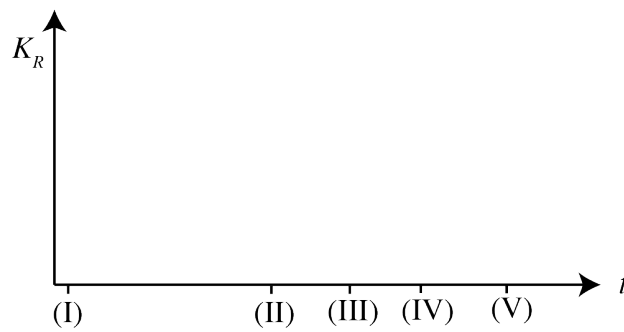
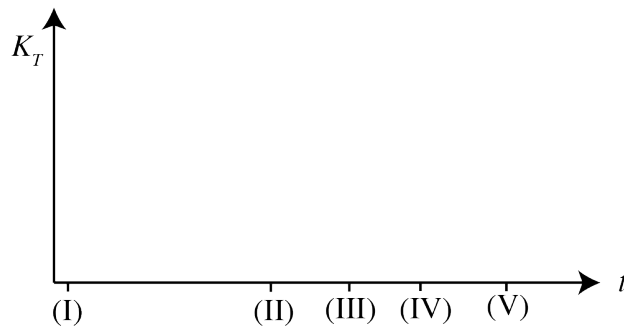
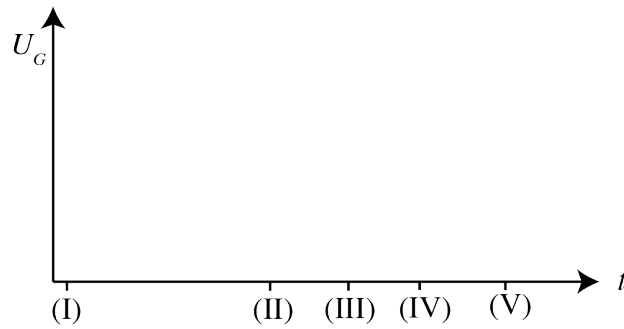
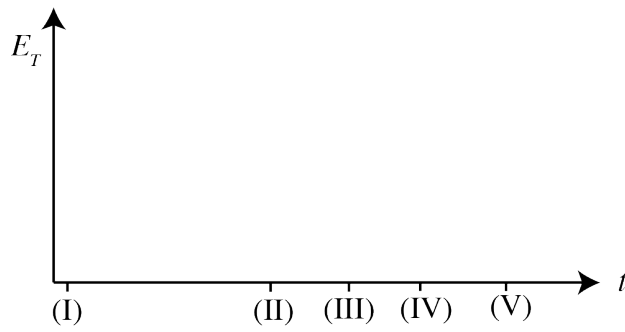


A.6 (0.4 pt)

$$\frac{dL_z}{dt} =$$

A.7 (1.4 pt)

$$\frac{dE_T}{dt} =$$

**A.8** (2.0 pt)



A.9 (0.5 pt)

$k =$

A.10 (1.7 pt)

$\mathbf{v} =$