EQ1: Official Solution[1]

A.1 (1.0 pt)
Move the magnet along each of the axes and notice the change in the magnet field. For example, if the magnet is aligned along the length of the phone, and you are moving the magnet along the same direction (length of the phone), magnetic field will show the change in sign when the magnet crosses the Magnetometer.

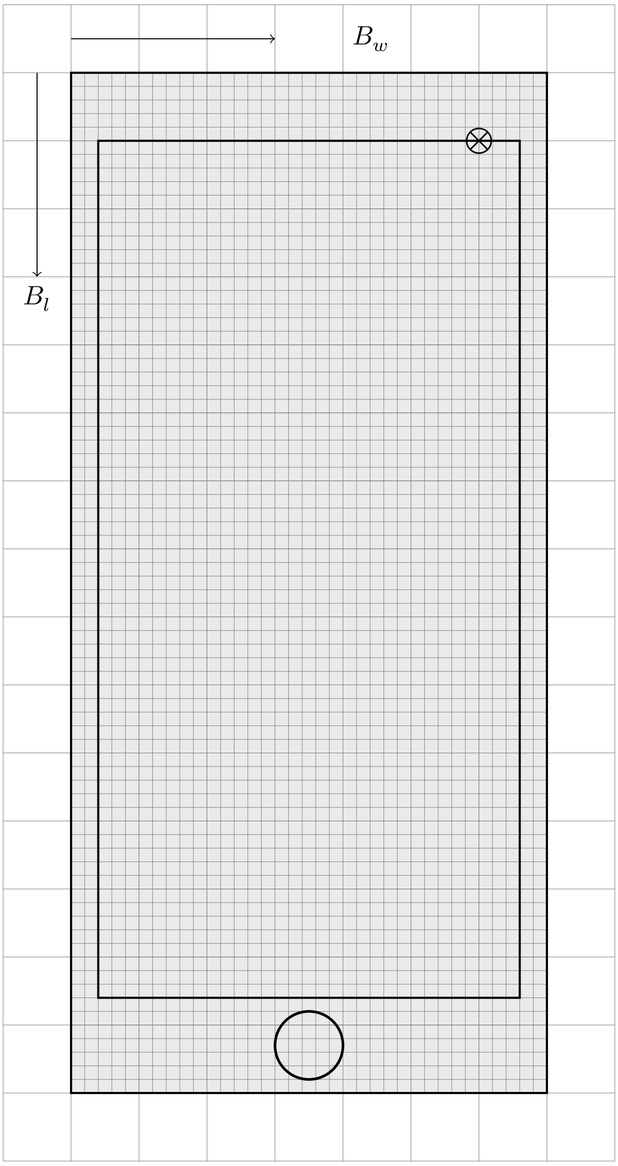
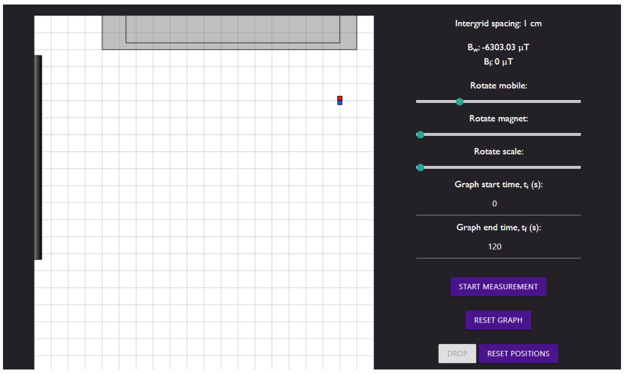


Figure. 1

[1] Chandan Relekar (IISc, Bangalore), Siddhant Mukherjee (The University of Cambridge, UK), Siddharth Tiwary (IIT Powai, Mumbai), Charudutt Kadolkar (IIT Guwahati), Praveen Pathak (HBCSE-TIFR, Mumbai), were the principal authors of this problem. The contributions of the Academic Committee and the International Board are gratefully acknowledged.

A.2 (2.3 pt)
The set up to find Dipole moment



The magnetic field B_w of a point dipole at the distance x $(x >> d)$ from the dipole's center can be approximated by

$$B_w = \frac{\mu_0}{2\pi}\frac{M}{x^3} \tag{1}$$

Rearranging above equation, we get

$$B_w = \frac{\mu_0 M}{2\pi} \times \frac{1}{x^3} \tag{2}$$

From equation (2), a plot of B_w vs $\dfrac{1}{x^3}$ is a straight line passing through origin. Solving the slope will give dipole moment of the magnet.

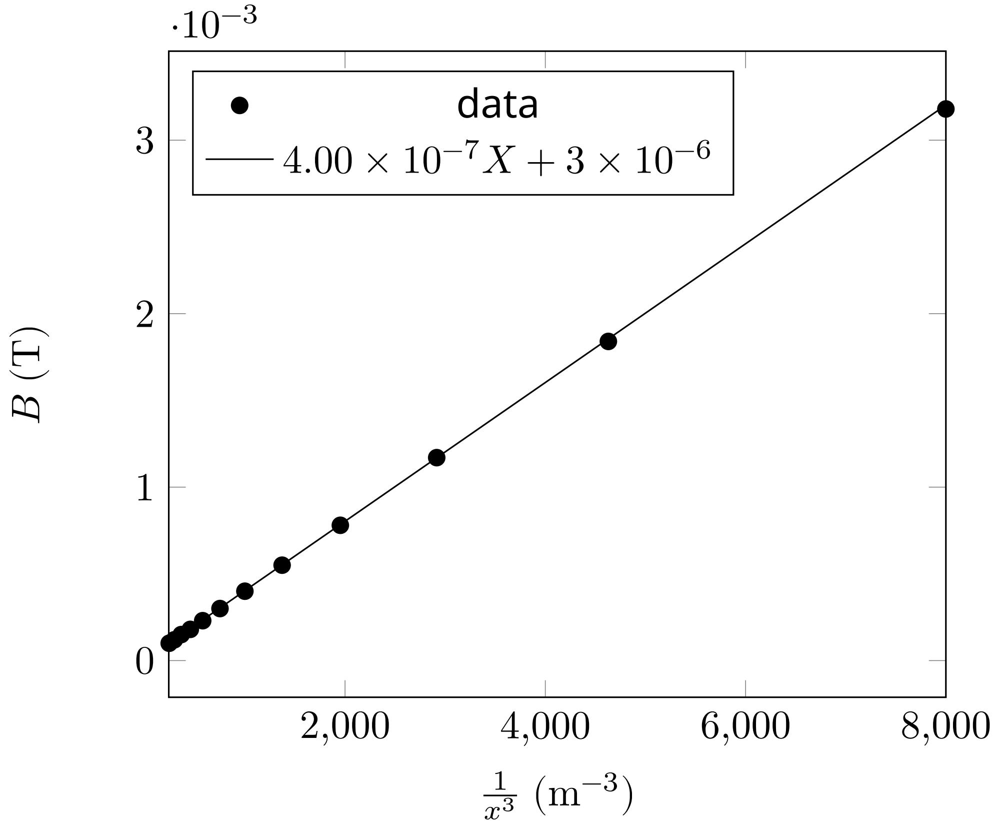
A.2 (cont.)
Dipole moment of the Magnet:
Fill the appropriate quantities.

Sr.No	x (cm)	$B_w (\mu\mathrm{T})$	$\frac{1}{x^3} (\mathrm{m}^{-3})$	B_w (T)
1	5	3177.63	8000	0.00317763
2	6	1841.06	4629.63	0.00184106
3	7	1170.34	2915.45	0.00117034
4	8	783.69	1953.13	0.00078369
5	9	550.22	1371.74	0.00055022
6	10	403.42	1000	0.00040342
7	11	301.21	751.31	0.00030121
8	12	231.96	578.7	0.00023197
9	13	181.58	455.17	0.00018158
10	14	146.03	364.43	0.00014603
11	15	118.72	296.3	0.00011872
12	16	98.18	244.14	0.000099

From equation (2), a plot of B_w vs $\dfrac{1}{x^3}$ is a straight line passing through the origin. The magnitude of the dipole moment can be calculated from the slope.

A.2 (cont.)

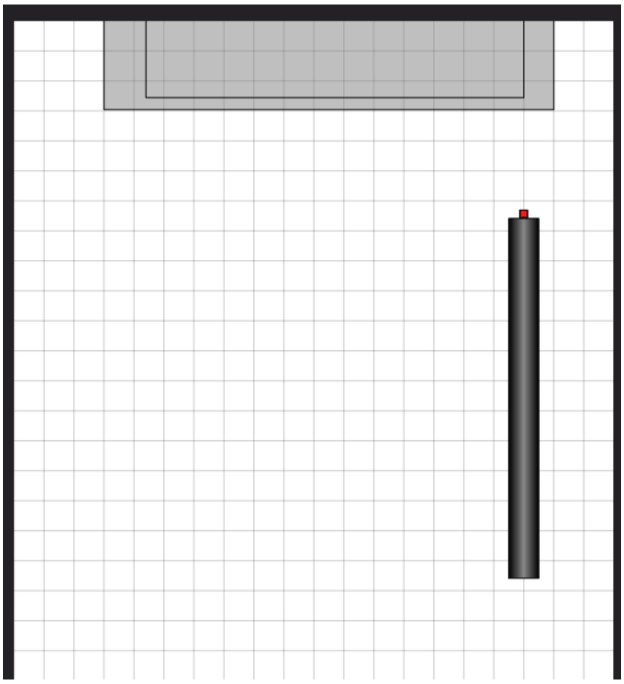
Graph of $\boxed{B_w}$ vs $\boxed{\frac{1}{x^3}}$



Slope of the graph: $4.00 \times 10^{-7}\ \mathrm{Nm}^2/\mathrm{A}$

Dipole moment of the magnet: 2.00 Am^2

B.1 (0.3 pt)
Rotate the smartphone and align the magnet and the pipe along the width of the phone as shown below.



Consider the case when the magnet is at rest at a distance x_0 from the magnetometer origin. The magnet is released along the axis of the pipe. It will start descending through the pipe. In the conducting sections of the pipe, after a brief period of accelerated motion, the magnet will attain a terminal velocity v, due to the presence of eddy current damping. In this case, the magnetic field B_w measured by the magnetometer changes with time t as

$$B_w(t) = \frac{\mu_0}{2\pi}\frac{M}{(x_0 + vt)^3} \tag{3}$$

Equation (3) is rearranged as

$$\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3} = vt + x_0 \tag{4}$$

B.1 (cont.)

Obtained profile of magnetic field vs time clearly suggests three distinct phases (AB, BC, and CD) of the magnet's motion (see Fig. 4 below).

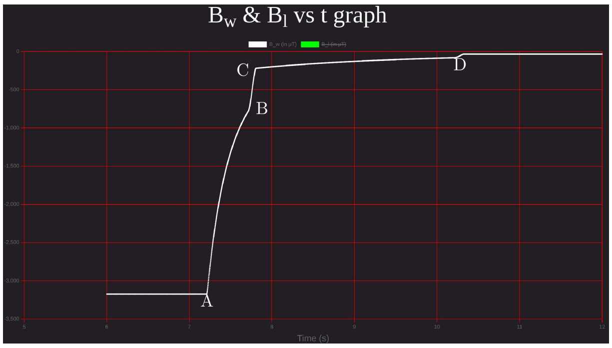


Figure (4)

We collect the data of (B_w vs t) for all three phases and plot them according to Eq. (4). For the acceleration phase of the pipe (wooden section), the graph will be non-linear and for the conducting pipe sections (Al and Cu) where the magnet moves with the terminal velocities, the graph will be linear. Duration of accelerated motion before attaining terminal velocity in the conducting sections of the pipe may be neglected.

It can be clearly seen from the graphs in the next sub parts that:

Section	Section number
Aluminium	1
Copper	3
wood	2

Since the copper has higher conductivity than aluminium, the terminal velocity in Cu section will be lower than Al section.

B.2 (2.6 pt)
Terminal velocity of Magnet in aluminium section:
Fill the appropriate quantities.

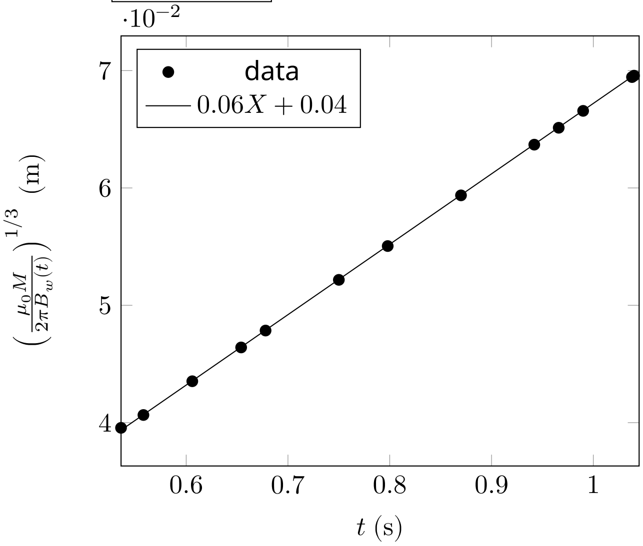
Sr.No	B_w (μT)	t (s)	$\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ (m)	v (m/s)
1	6462.28	0.534	0.0396	0
2	6462.28	0.536	0.0396	0.01
3	5954.24	0.558	0.0407	0.06
4	4850.05	0.606	0.0435	0.06
5	4002.02	0.654	0.0464	0.06
6	3651.48	0.678	0.0478	0.06
7	2817.43	0.75	0.0522	0.06
8	2397.97	0.798	0.055	0.06
9	1911.68	0.87	0.0594	0.06
10	1548.47	0.942	0.0637	0.06
11	1448.01	0.966	0.0651	0.06
12	1356.06	0.99	0.0666	0.06
13	1194.26	1.038	0.0694	0.06
14	1188.09	1.04	0.0696	0.14
15	1142.95	1.05	0.071	

The velocity (v) column is obtained using the forward difference $\dfrac{x_{n+1} - x_n}{t_{n+1} - t_n}$.

From equation (4), a plot of $\left(\dfrac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ vs t will be a straight line. The slope of the line will give terminal velocity .

B.2 (cont.)

Graph of $\boxed{\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}}$ vs $\boxed{t}$



Slope of the graph: $6\ \mathrm{cm/s}$.

Terminal velocity of the magnet in aluminium section: $6\ \mathrm{cm/s}$

Length of the aluminium section:

Slope of the graph: Not used

Intercept of the graph: Not used

Values in the fourth column in the above table actually represents the distance of the magnet from the magnetometer. We calculate the velocity (column 5) of the magnet using the forward difference method. Notice that the magnetic field starts to change at 0.536 s. Hence this is the point at which the magnet starts descending. It quickly achieves the terminal velocity of $6\ \mathrm{cm/s}$. A change in velocity (or departure from the flat line in v vs t curve, if you plot) occurs at 1.040 s. This suggests that the magnet moved out of the aluminium section of the pipe at this time.

Length of the Al section $= (1.040 - 0.536) \times 6\ \mathrm{cm} = 3.024\ \mathrm{cm}$.

B.3 (2.2 pt)
Terminal velocity of magnet in copper section:
Fill the appropriate quantities.

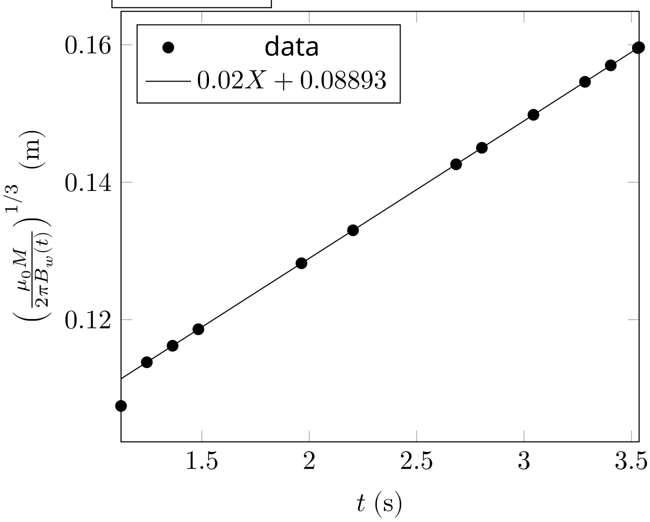
Sr.No	B_w (μT)	t (s)	$\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ (m)	v (m/s)
1	338.23	1.122	0.106	0.85
2	322.39	1.124	0.1075	0.87
3	271.32	1.244	0.1138	0.02
4	254.86	1.364	0.1162	0.02
5	239.70	1.484	0.1186	0.02
6	189.79	1.964	0.1282	0.02
7	169.97	2.204	0.1330	0.02
8	137.91	2.684	0.1426	0.02
9	131.17	2.804	0.1450	0.02
10	118.96	3.044	0.1498	0.02
11	108.22	3.284	0.1546	0.02
12	103.34	3.404	0.1570	0.02
13	98.52	3.53	0.1595	0.02
14	98.44	3.532	0.1596	0.02
15	98.37	3.534	0.1596	0.02
16	98.30	3.536	0.1597	0.05
17	98.22139	3.538	0.1597	

The velocity (v) column is obtained using the forward difference $\dfrac{x_{n+1} - x_n}{t_{n+1} - t_n}$.

From equation (4), a plot of $\left(\dfrac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ vs t will be a straight line. The slope of the line will give the terminal velocity.

B.3 (cont.)

Graph of $\boxed{\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}}$ vs $\boxed{t}$



Slope of the graph: $2\ \mathrm{cm/s}$.

Terminal velocity of magnet in copper section: $2\ \mathrm{cm/s}$

Length of copper section:

Slope of the graph: Not used

Intercept of the graph:Not used

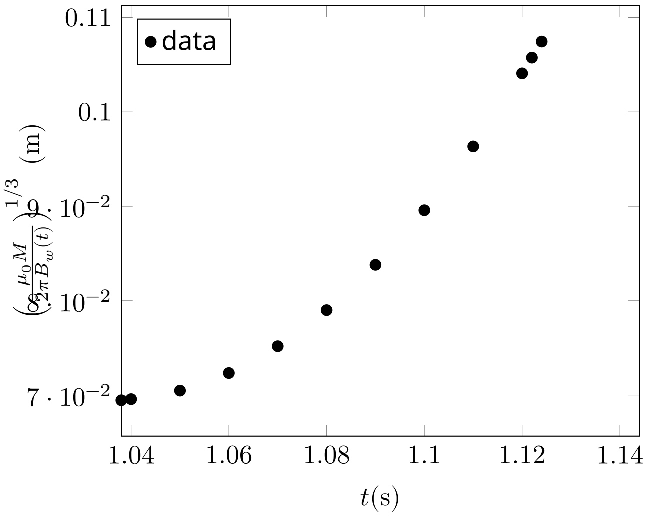
Length of the copper section of the pipe can be calculated by $v_c t_c$, where v_c is the terminal velocity of the magnet in the copper section of the pipe and t_c is the time spent by the magnet in the copper section of the pipe.
Data in the above table suggests that the magnet enters the copper section at $1.124\,\mathrm{s}$, and it leaves the copper section of the pipe at $3.536\,\mathrm{s}$ where we see sudden velocity change.
Length of the copper section $= (3.536 - 1.124) \times 2\ \mathrm{cm} = 4.824\,\mathrm{cm}$.

B.4 (1.6 pt)
Length of wooden section:
Fill the appropriate quantities.

Sr.No	B_w (μT)	t (s)	$\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ (m)	v (m/s)	a (m/s^2)
1	1194.26	1.038	0.0694	0.06	4
2	1188.09	1.04	0.070	0.14	5.66
3	1142.95	1.05	0.071	0.15	9.8
4	1056.94	1.06	0.072	0.25	9.8
5	941.55	1.07	0.075	0.34	9.8
6	811.40	1.08	0.079	0.44	9.8
7	679.75	1.09	0.084	0.54	9.8
8	556.44	1.1	0.090	0.64	9.8
9	447.31	1.11	0.096	0.74	9.8
10	354.74	1.12	0.104	0.83	9.8
11	338.23	1.122	0.106	0.85	-334.92
12	322.39	1.124	0.108	0.18	0.31
13	271.32	1.244	0.114		

The velocity (v) and acceleration (a) columns are obtained using the forward difference $\frac{x_{n+1} - x_n}{t_{n+1} - t_n}$ and $\frac{v_{n+1} - v_n}{t_{n+1} - t_n}$ respectively.

B.4 (cont.)



Wooden section is the middle section of the pipe. We have already established in Al section that the magnet exits the Al section at $1.040\ \mathrm{s}$. We tabulate the data of velocity vs time for this section. Notice that the velocity of the magnet suddenly drops at $1.124\ \mathrm{s}$. At this moment, the magnet enters in the copper section of the pipe and comes under the influence of damping due to the eddy current.

Length of the pipe can be calculated by $\left(v_{\mathrm{Al}} t_w + \frac{g t_w^2}{2}\right)$, where v_{Al} is terminal velocity of magnet in the aluminium section of the pipe and t_w is the time spent by the magnet in the wooden section of the pipe.

Total time spent by the magnet in the wooden pipe $(t_w) = (1.124 - 1.040)\ \mathrm{s} = 0.084\ \mathrm{s}$

Length of the wooden section of pipe $= 3.96\ \mathrm{cm}$

EQ1: Official Solution[1]

A.1 (1.0 pt)
Move the magnet along each of the axes and notice the change in the magnet field. For example, if the magnet is aligned along the length of the phone, and you are moving the magnet along the same direction (length of the phone), magnetic field will show the change in sign when the magnet crosses the Magnetometer.

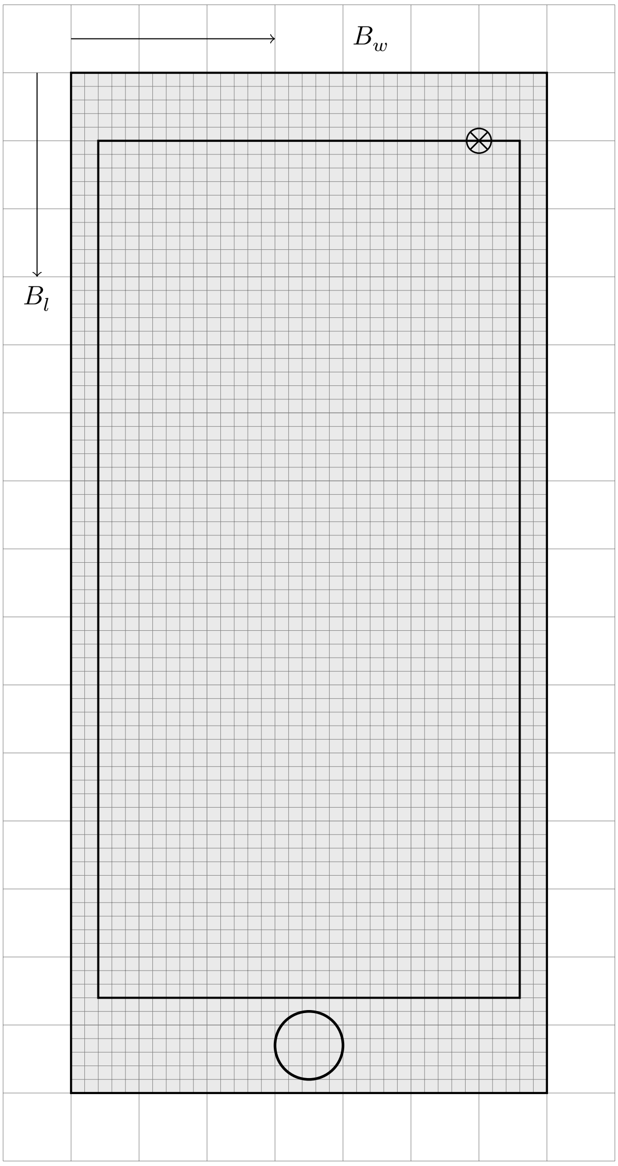


Figure. 1

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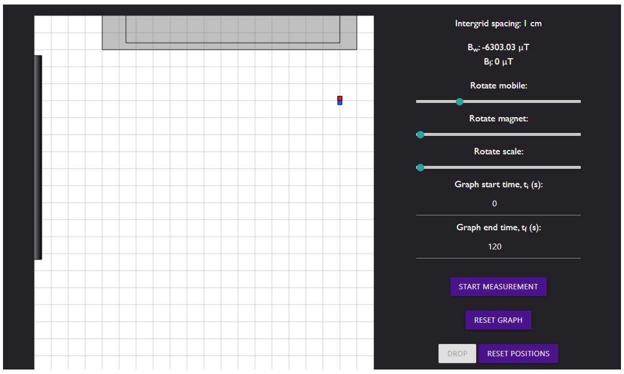
A.2 (2.3 pt)
The set up to find Dipole moment



The magnetic field B_w of a point dipole at the distance x $(x >> d)$ from the dipole's center can be approximated by

$$B_w = \frac{\mu_0}{2\pi}\frac{M}{x^3} \tag{1}$$

Rearranging above equation, we get

$$B_w = \frac{\mu_0 M}{2\pi} \times \frac{1}{x^3} \tag{2}$$

From equation (2), a plot of B_w vs $\dfrac{1}{x^3}$ is a straight line passing through origin. Solving the slope will give dipole moment of the magnet.

A.2 (cont.)

Dipole moment of the Magnet:

Fill the appropriate quantities.

Sr.No	x (cm)	$B_w (\mu\mathrm{T})$	$\frac{1}{x^3} (\mathrm{m}^{-3})$	B_w (T)
1	5	3177.63	8000	0.00317763
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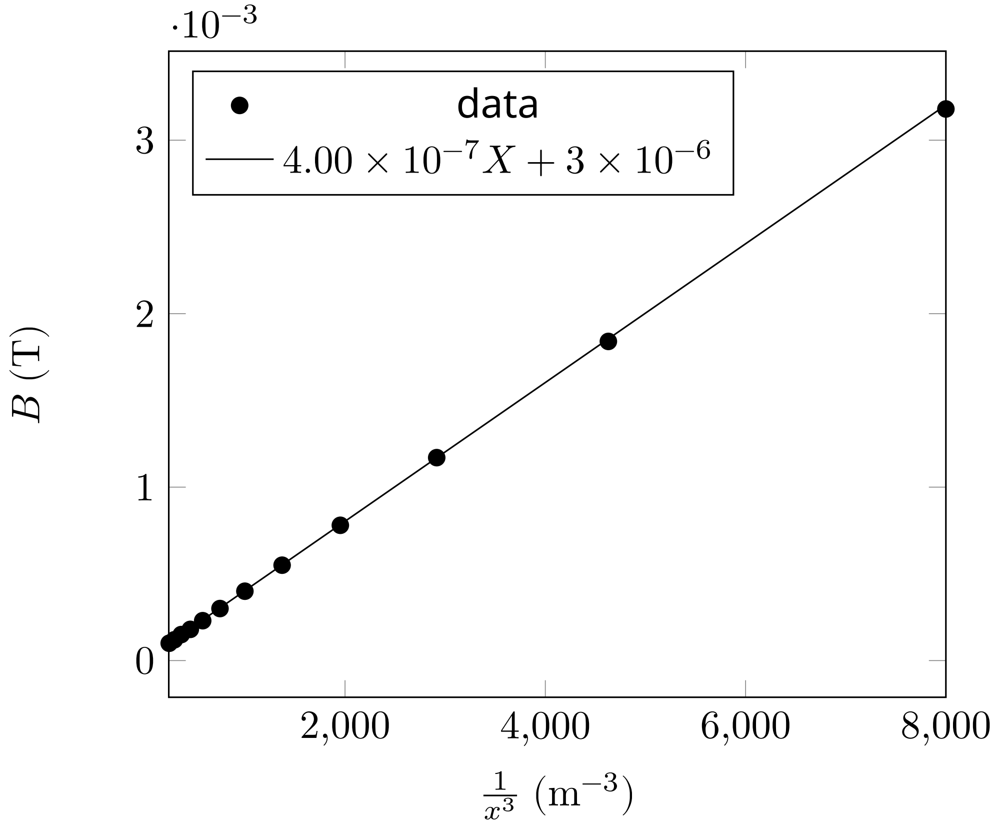
10	14	146.03	364.43	0.00014603
11	15	118.72	296.3	0.00011872
12	16	98.18	244.14	0.000099

From equation (2), a plot of B_w vs $\dfrac{1}{x^3}$ is a straight line passing through the origin. The magnitude of the dipole moment can be calculated from the slope.

A.2 (cont.)

Graph of $\boxed{B_w}$ vs $\boxed{\frac{1}{x^3}}$



Slope of the graph: $4.00 \times 10^{-7}\ \mathrm{Nm^2/A}$

Dipole moment of the magnet: 2.00 $\mathrm{Am^2}$

B.1 (0.3 pt)
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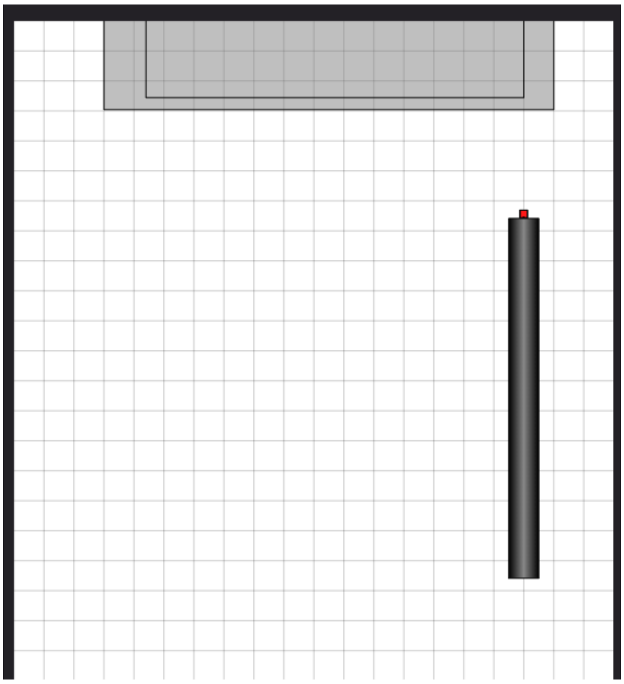


Consider the case when the magnet is at rest at a distance x_0 from the magnetometer origin. The magnet is released along the axis of the pipe. It will start descending through the pipe. In the conducting sections of the pipe, after a brief period of accelerated motion, the magnet will attain a terminal velocity v, due to the presence of eddy current damping. In this case, the magnetic field B_w measured by the magnetometer changes with time t as

$$B_w(t) = \frac{\mu_0}{2\pi}\frac{M}{(x_0 + vt)^3} \tag{3}$$

Equation (3) is rearranged as

$$\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3} = vt + x_0 \tag{4}$$

B.1 (cont.)
Obtained profile of magnetic field vs time clearly suggests three distinct phases (AB, BC, and CD) of the magnet's motion (see Fig. 4 below).

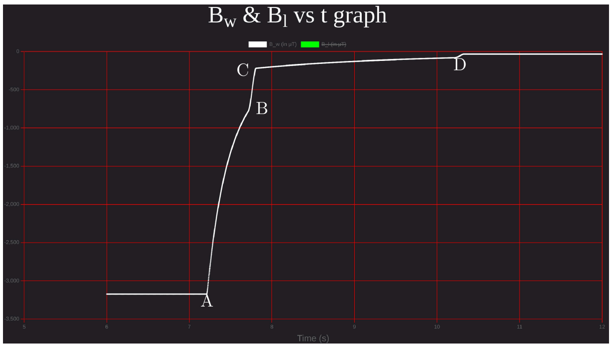


Figure (4)

We collect the data of (B_w vs t) for all three phases and plot them according to Eq. (4). For the acceleration phase of the pipe (wooden section), the graph will be non-linear and for the conducting pipe sections (Al and Cu) where the magnet moves with the terminal velocities, the graph will be linear. Duration of accelerated motion before attaining terminal velocity in the conducting sections of the pipe may be neglected.
It can be clearly seen from the graphs in the next sub parts that:

Section	Section number
Aluminium	1
Copper	3
wood	2

Since the copper has higher conductivity than aluminium, the terminal velocity in Cu section will be lower than Al section.

B.2 (2.6 pt)
Terminal velocity of Magnet in aluminium section:
Fill the appropriate quantities.

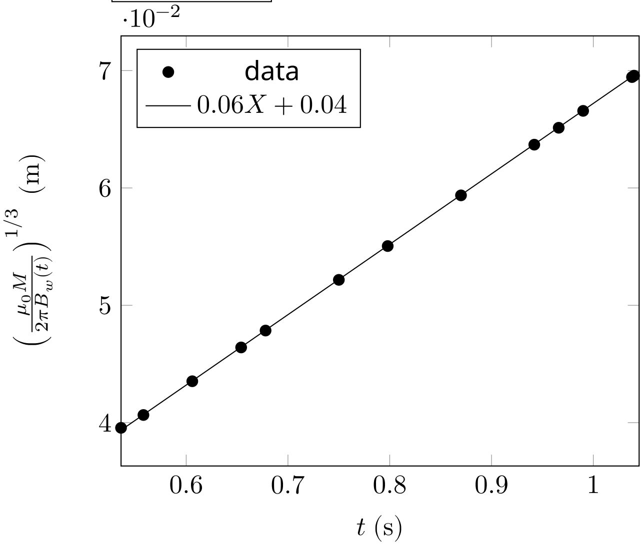
Sr.No	B_w (μT)	t (s)	$\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ (m)	v (m/s)
1	6462.28	0.534	0.0396	0
2	6462.28	0.536	0.0396	0.01
3	5954.24	0.558	0.0407	0.06
4	4850.05	0.606	0.0435	0.06
5	4002.02	0.654	0.0464	0.06
6	3651.48	0.678	0.0478	0.06
7	2817.43	0.75	0.0522	0.06
8	2397.97	0.798	0.055	0.06
9	1911.68	0.87	0.0594	0.06
10	1548.47	0.942	0.0637	0.06
11	1448.01	0.966	0.0651	0.06
12	1356.06	0.99	0.0666	0.06
13	1194.26	1.038	0.0694	0.06
14	1188.09	1.04	0.0696	0.14
15	1142.95	1.05	0.071	

The velocity (v) column is obtained using the forward difference $\frac{x_{n+1} - x_n}{t_{n+1} - t_n}$.

From equation (4), a plot of $\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ vs t will be a straight line. The slope of the line will give terminal velocity .

B.2 (cont.)

Graph of $\boxed{\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}}$ vs $\boxed{t}$



Slope of the graph: $6\ \mathrm{cm/s}$.

Terminal velocity of the magnet in aluminium section: $6\ \mathrm{cm/s}$

Length of the aluminium section:

Slope of the graph: Not used | Intercept of the graph: Not used

Values in the fourth column in the above table actually represents the distance of the magnet from the magnetometer. We calculate the velocity (column 5) of the magnet using the forward difference method. Notice that the magnetic field starts to change at 0.536 s. Hence this is the point at which the magnet starts descending. It quickly achieves the terminal velocity of $6\ \mathrm{cm/s}$. A change in velocity (or departure from the flat line in v vs t curve, if you plot) occurs at 1.040 s. This suggests that the magnet moved out of the aluminium section of the pipe at this time.

Length of the Al section $= (1.040 - 0.536) \times 6\ \mathrm{cm} = 3.024\ \mathrm{cm}$.

B.3 (2.2 pt)
Terminal velocity of magnet in copper section:
Fill the appropriate quantities.

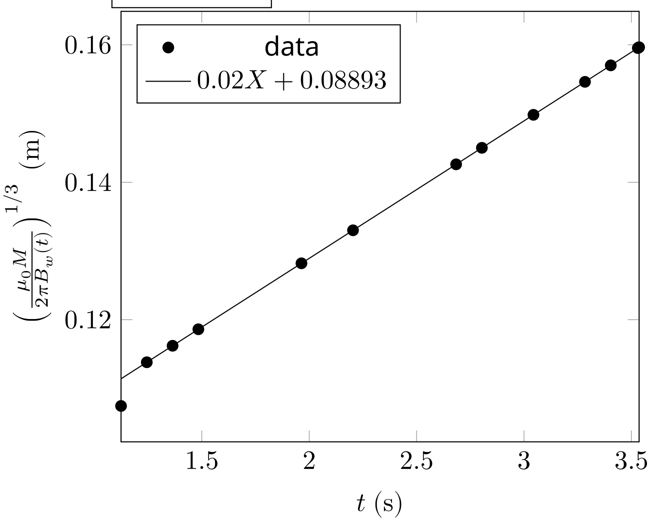
Sr.No	B_w (μT)	t (s)	$\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ (m)	v (m/s)
1	338.23	1.122	0.106	0.85
2	322.39	1.124	0.1075	0.87
3	271.32	1.244	0.1138	0.02
4	254.86	1.364	0.1162	0.02
5	239.70	1.484	0.1186	0.02
6	189.79	1.964	0.1282	0.02
7	169.97	2.204	0.1330	0.02
8	137.91	2.684	0.1426	0.02
9	131.17	2.804	0.1450	0.02
10	118.96	3.044	0.1498	0.02
11	108.22	3.284	0.1546	0.02
12	103.34	3.404	0.1570	0.02
13	98.52	3.53	0.1595	0.02
14	98.44	3.532	0.1596	0.02
15	98.37	3.534	0.1596	0.02
16	98.30	3.536	0.1597	0.05
17	98.22139	3.538	0.1597	

The velocity (v) column is obtained using the forward difference $\dfrac{x_{n+1} - x_n}{t_{n+1} - t_n}$.

From equation (4), a plot of $\left(\dfrac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ vs t will be a straight line. The slope of the line will give the terminal velocity.

B.3 (cont.)

Graph of $\boxed{\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}}$ vs $\boxed{t}$



Slope of the graph: $2\ \mathrm{cm/s}$.

Terminal velocity of magnet in copper section: $2\ \mathrm{cm/s}$

Length of copper section:

Slope of the graph: Not used

Intercept of the graph:Not used

Length of the copper section of the pipe can be calculated by $v_c t_c$, where v_c is the terminal velocity of the magnet in the copper section of the pipe and t_c is the time spent by the magnet in the copper section of the pipe.
Data in the above table suggests that the magnet enters the copper section at $1.124\,\mathrm{s}$, and it leaves the copper section of the pipe at $3.536\,\mathrm{s}$ where we see sudden velocity change.
Length of the copper section $= (3.536 - 1.124) \times 2\ \mathrm{cm} = 4.824\,\mathrm{cm}$.

B.4 (1.6 pt)

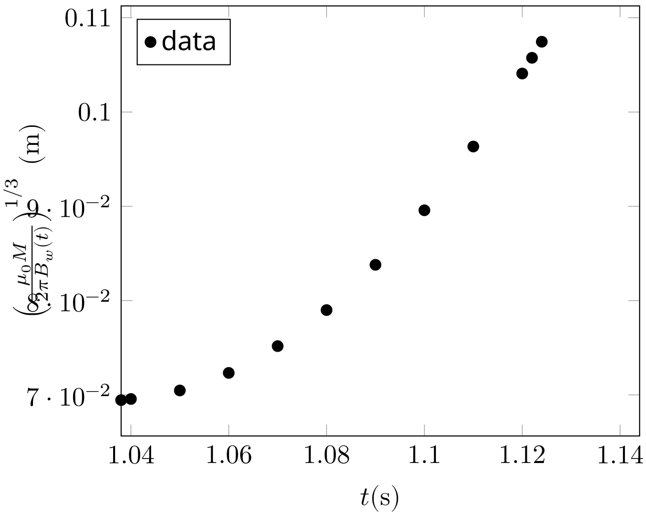
Length of wooden section:

Fill the appropriate quantities.

Sr.No	B_w (μT)	t (s)	$\left(\frac{\mu_0 M}{2\pi B_w(t)}\right)^{1/3}$ (m)	v (m/s)	a (m/s^2)
1	1194.26	1.038	0.0694	0.06	4
2	1188.09	1.04	0.070	0.14	5.66
3	1142.95	1.05	0.071	0.15	9.8
4	1056.94	1.06	0.072	0.25	9.8
5	941.55	1.07	0.075	0.34	9.8
6	811.40	1.08	0.079	0.44	9.8
7	679.75	1.09	0.084	0.54	9.8
8	556.44	1.1	0.090	0.64	9.8
9	447.31	1.11	0.096	0.74	9.8
10	354.74	1.12	0.104	0.83	9.8
11	338.23	1.122	0.106	0.85	-334.92
12	322.39	1.124	0.108	0.18	0.31
13	271.32	1.244	0.114		

The velocity (v) and acceleration (a) columns are obtained using the forward difference $\frac{x_{n+1} - x_n}{t_{n+1} - t_n}$ and $\frac{v_{n+1} - v_n}{t_{n+1} - t_n}$ respectively.

B.4 (cont.)



Wooden section is the middle section of the pipe. We have already established in Al section that the magnet exits the Al section at $1.040\ \mathrm{s}$. We tabulate the data of velocity vs time for this section. Notice that the velocity of the magnet suddenly drops at $1.124\ \mathrm{s}$. At this moment, the magnet enters in the copper section of the pipe and comes under the influence of damping due to the eddy current.

Length of the pipe can be calculated by $\left(v_{\mathrm{Al}} t_w + \frac{g t_w^2}{2}\right)$, where v_{Al} is terminal velocity of magnet in the aluminium section of the pipe and t_w is the time spent by the magnet in the wooden section of the pipe.

Total time spent by the magnet in the wooden pipe $(t_w) = (1.124 - 1.040)\ \mathrm{s} = 0.084\ \mathrm{s}$

Length of the wooden section of pipe $= 3.96\ \mathrm{cm}$

Section	EQ1: Magnetic black box marking scheme	Partwise marks		Total
				marks
A1	Identifying correct location of the inbuilt sensor (full marks if both the coordinates correct within ± 0.2 cm, else no credit	**1.0**		**1.0 pt**
A2				**2.3 pt**
	Choice of variables for plotting	**0.1**		
	Units on these variables	**0.1**		
	For observations of x and B	***(0.8)***		
	less than 5 readings		0	
	5 readings		0.5	
	6 readings		0.6	
	7 readings		0.7	
	8 or more readings	0.8		
	Calculation of quantities to be plotted (full marks only if calculations are correct for all points, else no credit)	**0.1**		
	Graph	**(0.8)**		
	Choice of Scale (minimum 70% coverage)	0.2		
	Both axes labelled with proper units	0.2		
	At least 8 points plotted correctly	0.3		
	At least 6 points plotted correctly		0.1	
	Less than 6 points plotted		0	
	Best fit	0.1		
	Value of dipole moment (Deduct 0.1 for wrong or no unit)	**(0.4)**		
	Between 1.9 and 2.1 Am^2	0.4		
	1.8 to less than 1.9 and greater than 2.1 upto 2.2 Am^2		0.2	

Section		Partwise marks	Total marks
B1	Predicting the sections in correct order	**0.3**	**0.3 pt**
B2			**2.6 pt**
	Schematic diagram of set up (exact location and orientation)	**0.1**	
	Choice of variables for plotting	**0.3**	
	For observations of t and B	**(0.3)**	
	less than 7 readings	0	
	7 to 9 readings	0.2	
	10 or more readings	0.3	
	Calculation of quantities to be plotted (full marks only if calculations are correct for all points, else no credit)	**0.3**	
	Graph	**(1.0)**	
	Choice of Scale (minimum 70% coverage)	0.2	
	Both axes labelled with proper units	0.1	
	At least 10 points plotted correctly	0.5	
	8 or 9 points plotted correctly	0.4	
	6 or 7 points plotted correctly	0.3	
	Best fit	0.2	
	Value of terminal velocity (Deduct 0.1 for wrong or no unit)	**(0.2)**	
	Between 5.9 and 6.1 cm/s	0.2	
	5.8 to less than 5.9 cm/s OR greater than 6.1 upto 6.2 cm/s	0.1	
	Determination of length of aluminium section	**(0.4)**	
	Between 2.9 and 3.1 cm	0.4	
	2.8 to less than 2.9 cm OR greater than 3.1 upto 3.2 cm	0.2	

B3			2.2 pt
	For observations of t and B	(0.3)	
	less than 7 readings	0	
	7 to 9 readings	0.2	
	10 or more readings	0.3	
	Calculation of quantities to be plotted (full marks only if calculations are correct for all points, else no credit)	**0.3**	
	Graph	**(1.0)**	
	Choice of Scale (minimum 70% coverage)	0.2	
	Both axes labelled with proper units	0.1	
	At least 10 points plotted correctly	0.5	
	8 or 9 points plotted correctly	0.4	
	6 or 7 points plotted	0.3	
	Best fit	0.2	
	Value of terminal velocity (Deduct 0.1 for wrong or no unit)	**(0.2)**	
	Between 1.9 and 2.1 cm/s	0.2	
	1.8 to less than 1.9 cm/s OR greater than 2.1 upto 2.2 cm/s	0.1	
	Determination of length of copper section (Deduct 0.1 for wrong or no unit)	**(0.4)**	
	Between 4.9 and 5.1 cm	0.4	
	4.8 to less than 4.9 cm and greater than 5.1 upto 5.2cm	0.2	

B4 (Method I)	Length of the wooden section of pipe		**1.6 pt**
By drawing graph			
	Choice of variables	**0.1**	
	Units of variables	**0.2**	
	For observations of t and B	**(0.3)**	
	6 to 9 readings	0.2	
	10 or more readings	0.3	
	Calculations of function (determination of acceleration OR Graph plotting)	**(0.6)**	
	If all correct	0.6	
	50% correct	0.3	
	Less than 50% correct	0	
	Determination of length of wooden section (deduct 0.1 for wrong or no unit)	**(0.4)**	
B 4 (Method II) **Using the terminal velocity in Al part, time of free fall and g**	To determine $t = t_w$	**(1.3)**	
	$t = t_w$ *= 0.082 s to 0.086 s*	1.3	
	0.08 s t_w *<0.082 s OR*	0.6	
	0.086 s <t_w *0.088 s*		
	Calculation of L_w as per student's value of t (Deduct 0.1 for wrong or no unit)	**0.3**	
B4 (Method III)	3.9 ≤Length ≤4.1	1.6	**1.6 pt**
By subtracting the lengths			
	Length between 4.2-4.1 and 4.1-4.2 ≤4.1	**0.6**	

EQ2: Acoustic black box marking Scheme			
Section		**Partwise marks**	**Total**
A1	**finding expression of** $x_(t)$ **and** $y_(t)$		**0.2**
A2	**Plotting graph of** $f_{\min}$ **vs** t		**1.2**
	Choice of scale (70% coverage)	0.2	
	Both axis labelled with proper units	0.2	
	More than 8 points labelled correctly	either 0.4	
	Atleast 5-7 points plotted	or 0.2	
	Less than 5 points plotted	**No Credit**	
	Data table		
	10 points reported correctly	either 0.4	
	6-9 points reported correctly	or 0.2	
	Less than 6 points reported	**No Credit**	
A3	**Evaluating expression of eventual** $f_{\min}$(No partial marking)		**1**
A4	**Determination of source's coordinates**		**1.4**
	idea of triangulation (i.e. getting the equations correctly)	**1**	
	correct value of Δt_{x1} and Δt_{x2}	0.1+0.1	
	Final calculation of X_A and Y_A	0.1+0.1	
A5	**Calculating** f_0, ω, R, v_s		**2.1**
	Logic asymptotic values	0.3	
	Getting the retarded time expression correctly	0.6	
	Value of ω	0.2	
	expression of $f_{\max}$ and $f_{\min}$ for source moving away	0.3	
	expression of $f_{\max}$ and $f_{\min}$ for source moving towards	0.3	
	Determination of correct $f_{\max}$ and $f_{\min}$ for calculation	0.2	
	If all values correct f_0, R,v_s	either 0.2	
	If only two or one value is correct	or 0.1	

ABB Marking Scheme			
A6	**Finding angle β**		**2**
	Calculation of largest maximum frequency at some angle	0.6	
	Reporting data of extrema at various θ	0.4	
	Determination of the coordinates of D	0.4	
	Determination of Coordinates of E	0.4	
	Final calculation of β	0.2	
A7	**Finding centre coordinates**		**2.1**
	Expression of $f(t')$	1	
	If t' and t are same	-0.5	
	Determination of α	0.4	
	Determination of ϕ	0.4	
	coordinates of centre of circle	0.3	