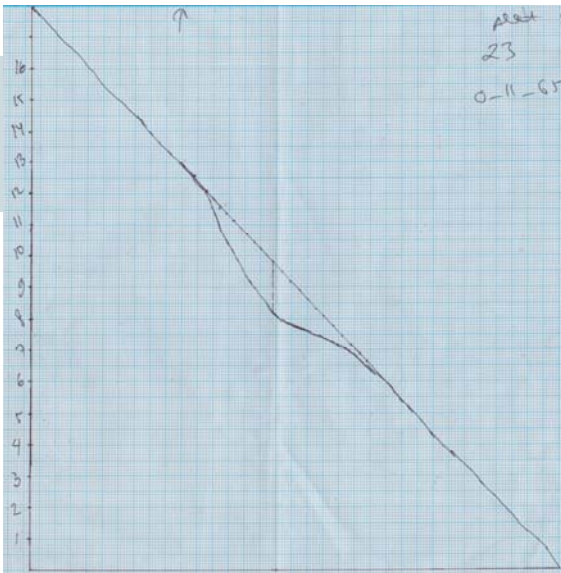


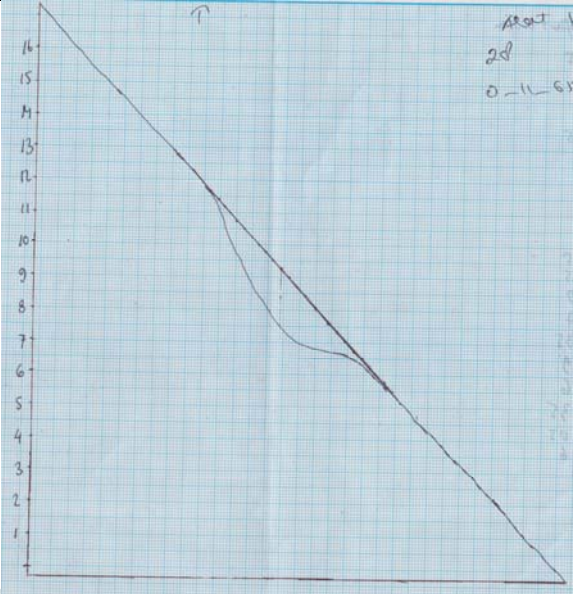
Determination of Refractive Index Gradient and Diffusion Coefficient of Salt Solution from Laser Deflection Measurement

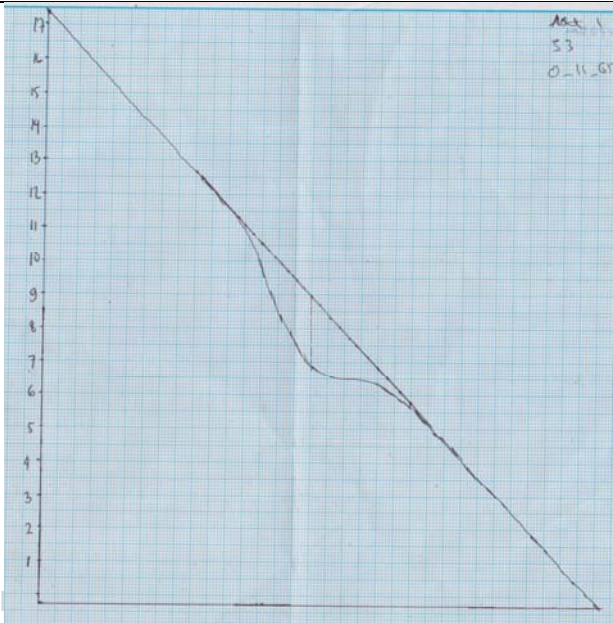
(10 points)

A. Measurement of Refractive Index Gradient of Salt Water Solution

(4.5 points)

Question	Answer	Marks
A1. (1.2 pts)	 No dip No reference line Deflectogram (DL) not at the centre (+- 5mm) but the depth of dip still in 1.5 - 1.6 cm range DL at the centre, the depth of dip <1.5 cm or >1.6 cm DL not at the centre, the depth of dip <1.5 cm or >1.6 cm	Deflectogram of $C_0 = 23 \text{ g/150 mL}$ Centred Depth of dip: 1.5 - 1.6 cm (0.4 pts) -0.4 -0.05 -0.05 -0.05 -0.1
		Deflectogram

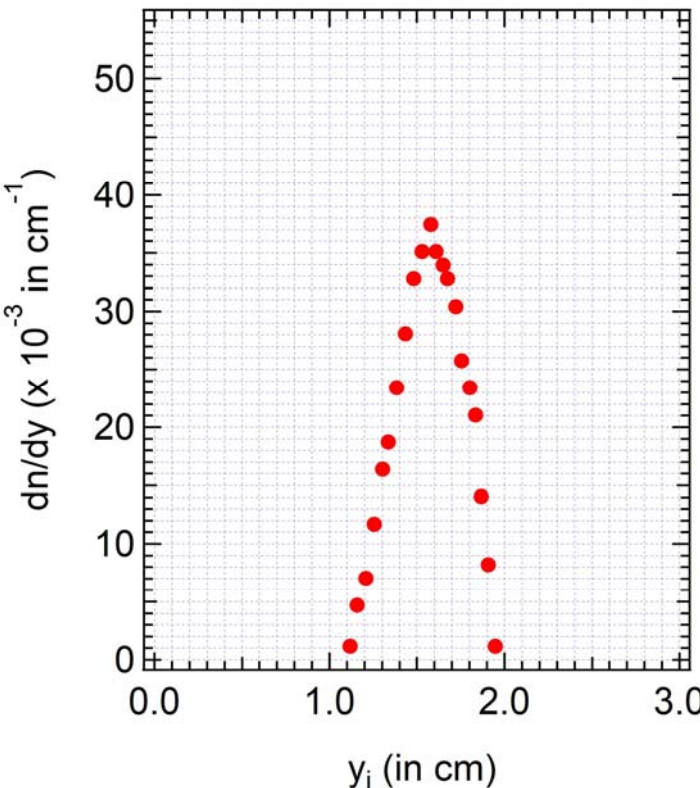
A1.	 No dip No reference line Deflectogram (DL) not at the centre (± 5 mm) but the depth of dip still in 1.7 cm - 1.9 cm range DL at the centre, the depth of dip < 1.7 cm or > 1.9 cm DL not at the centre, the depth of dip < 1.7 cm or > 1.9 cm	of $C_0 = 28 \text{ gr}/150 \text{ mL}$ Centred Deep of dip: 1.7 - 1.9 cm (0.4 pts) -0.4 -0.05 -0.05 -0.05 -0.1
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A1.	 No dip No reference line Deflectogram (DL) not at the centre (+5mm) but the depth of dip still in 1.9 - 2.3 cm range DL at the centre, the depth of dip <1.9 cm or >2.3 cm DL not at the centre, the depth of dip <1.9 cm or >2.3 cm	Deflectogram of $C_0 = 33 \text{ g/150 mL}$ Deep of dip: 1.9 - 2.3 cm (0.4 pts) -0.4 pts -0.05 pts - 0.05 pts - 0.05 pts -0.1																																																																																																
A2. (1.5 pts)	<table><tr><th>i</th><th>δ_i (cm)</th><th>ξ_i (cm)</th><th>Z_0 (cm)</th><th>d(cm)</th><th>Z (cm)</th></tr><tr><td>1</td><td>0.05</td><td>11.55</td><td>10.4 ± 0.1</td><td>0.8 ± 0.1</td><td>53.4 ± 0.1</td></tr><tr><td>2</td><td>0.35</td><td>11.3</td><td></td><td></td><td></td></tr><tr><td>3</td><td>0.6</td><td>11.05</td><td></td><td></td><td></td></tr><tr><td>4</td><td>0.9</td><td>10.85</td><td></td><td></td><td></td></tr><tr><td>5</td><td>1</td><td>10.65</td><td></td><td></td><td></td></tr><tr><td>6</td><td>1.1</td><td>10.35</td><td></td><td></td><td></td></tr><tr><td>7</td><td>1.3</td><td>10.15</td><td></td><td></td><td></td></tr><tr><td>8</td><td>1.4</td><td>9.85</td><td></td><td></td><td></td></tr><tr><td>9</td><td>1.45</td><td>9.7</td><td></td><td></td><td></td></tr><tr><td>10</td><td>1.5</td><td>9.45</td><td></td><td></td><td></td></tr><tr><td>11</td><td>1.6</td><td>9.25</td><td></td><td></td><td></td></tr><tr><td>12</td><td>1.5</td><td>8.95</td><td></td><td></td><td></td></tr><tr><td>13</td><td>1.4</td><td>8.65</td><td></td><td></td><td></td></tr><tr><td>14</td><td>1.2</td><td>8.35</td><td></td><td></td><td></td></tr><tr><td>15</td><td>1</td><td>8.05</td><td></td><td></td><td></td></tr></table>	i	δ_i (cm)	ξ_i (cm)	Z_0 (cm)	d (cm)	Z (cm)	1	0.05	11.55	10.4 ± 0.1	0.8 ± 0.1	53.4 ± 0.1	2	0.35	11.3				3	0.6	11.05				4	0.9	10.85				5	1	10.65				6	1.1	10.35				7	1.3	10.15				8	1.4	9.85				9	1.45	9.7				10	1.5	9.45				11	1.6	9.25				12	1.5	8.95				13	1.4	8.65				14	1.2	8.35				15	1	8.05				Table 1 of $C_0 = 23 \text{ g/150 mL}$ Optimum Z and Z_0 # data = 20 (0.5 pts)
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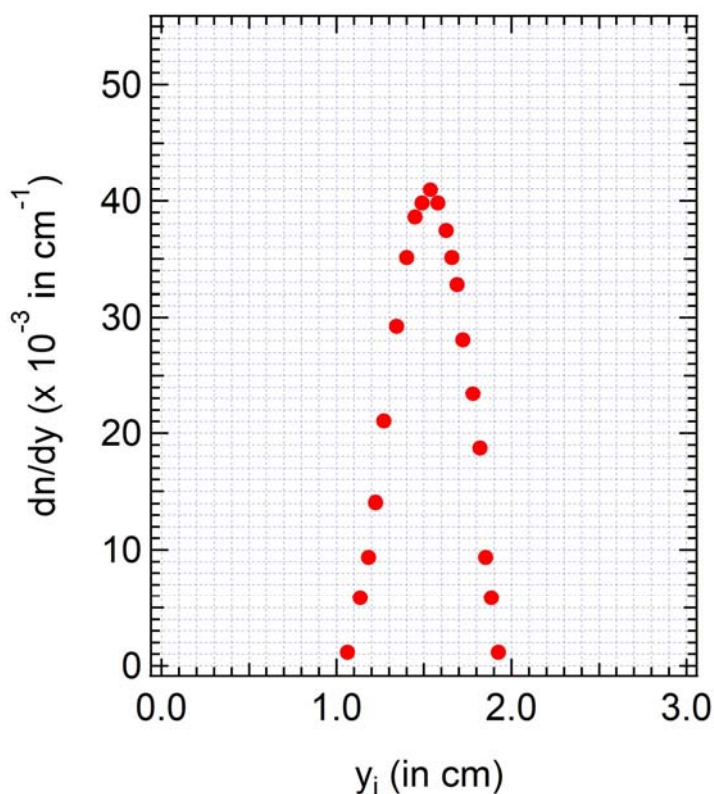
	<table><tr><td>16</td><td>0.8</td><td>7.75</td><td></td><td></td><td></td></tr><tr><td>17</td><td>0.7</td><td>7.55</td><td></td><td></td><td></td></tr><tr><td>18</td><td>0.5</td><td>7.25</td><td></td><td></td><td></td></tr><tr><td>19</td><td>0.3</td><td>6.95</td><td></td><td></td><td></td></tr><tr><td>20</td><td>0.2</td><td>6.65</td><td></td><td></td><td></td></tr><tr><td>21</td><td>0.05</td><td>6.4</td><td></td><td></td><td></td></tr></table> Correct data point must be extracted from deflectogram # correct data points ≥ 20, but not all observable (Z, Z_0, d) are written Incorrect d $15 \leq \# \text{ correct data points} < 20$, $10 < \# \text{ correct data points} < 15$ #correct data points < 10	16	0.8	7.75				17	0.7	7.55				18	0.5	7.25				19	0.3	6.95				20	0.2	6.65				21	0.05	6.4				-0.05 pts -0.05 pts -0.15 pts -0.3 pts -0.45 pts																																																																																										
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21	1.03034	0.00117																																																																		

A3.	 No x-axis label No x-axis unit Without x-axis unit No y-axis label No y-axis unit Without y-axis unit Ordinate axis represented in 2 digid behind point Ordinate axis represented in 3 digid behind point Random shape	Plot dn/dY vs Y $C_0 = 23 \text{ g/150 mL}$. “Gaussian-Like” shape (0.25 pts) -0.01 pts -0.01 pts -0.01 pts -0.01 pts -0.01 pts -0.01 pts -0.05 pts -0 pts -0.25 pts															
A3.	<table border="1" data-bbox="405 1839 788 2011"> <thead> <tr> <th>i</th><th>Y_i (cm)</th><th>dn/dY</th></tr> </thead> <tbody> <tr> <td>1</td><td>1.87554</td><td>0.00117</td></tr> <tr> <td>2</td><td>1.83529</td><td>0.00585</td></tr> <tr> <td>3</td><td>1.80309</td><td>0.00936</td></tr> <tr> <td>4</td><td>1.77089</td><td>0.01872</td></tr> </tbody> </table>	i	Y_i (cm)	dn/dY	1	1.87554	0.00117	2	1.83529	0.00585	3	1.80309	0.00936	4	1.77089	0.01872	Table 2 of $C_0 = 28 \text{ g/150 mL}$. # data = 20
i	Y_i (cm)	dn/dY															
1	1.87554	0.00117															
2	1.83529	0.00585															
3	1.80309	0.00936															
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	<table><tr><td>5</td><td>1.73065</td><td>0.02340</td></tr><tr><td>6</td><td>1.67430</td><td>0.02809</td></tr><tr><td>7</td><td>1.64210</td><td>0.03277</td></tr><tr><td>8</td><td>1.60990</td><td>0.03511</td></tr><tr><td>9</td><td>1.57770</td><td>0.03745</td></tr><tr><td>10</td><td>1.52941</td><td>0.03979</td></tr><tr><td>11</td><td>1.48916</td><td>0.04096</td></tr><tr><td>12</td><td>1.44086</td><td>0.03979</td></tr><tr><td>13</td><td>1.40061</td><td>0.03862</td></tr><tr><td>14</td><td>1.35232</td><td>0.03511</td></tr><tr><td>15</td><td>1.29597</td><td>0.02926</td></tr><tr><td>16</td><td>1.22352</td><td>0.02106</td></tr><tr><td>17</td><td>1.17523</td><td>0.01404</td></tr><tr><td>18</td><td>1.13498</td><td>0.00936</td></tr><tr><td>19</td><td>1.08668</td><td>0.00585</td></tr><tr><td>20</td><td>1.01424</td><td>0.00117</td></tr></table>	5	1.73065	0.02340	6	1.67430	0.02809	7	1.64210	0.03277	8	1.60990	0.03511	9	1.57770	0.03745	10	1.52941	0.03979	11	1.48916	0.04096	12	1.44086	0.03979	13	1.40061	0.03862	14	1.35232	0.03511	15	1.29597	0.02926	16	1.22352	0.02106	17	1.17523	0.01404	18	1.13498	0.00936	19	1.08668	0.00585	20	1.01424	0.00117	(0.25 pts)
5	1.73065	0.02340																																																
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	48TH IPHO 2017 YOGYAKARTA-INDONESIA 16 - 24 JULY 2017 Jury must check the data in table # wrong data point < 3 3<# wrong data point < 6 # wrong data point > 6	- 0 - 0.05 pts - 0.25pts																																																
A3.		Plot dn/dY vs Y $C_0 = 28 \text{ g/150 mL}$. “Gaussian-Like” shape (0.25 pts)																																																



without x-axis label

without x-axis unit

wrong x-axis unit

without y-axis label

without y-axis unit

wrong y-axis unit

Ordinate axis represented in 2 digid behind point

Ordinate axis represented in 3 digid behind point

Random shape of the curve

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.05 pts

-0 pts

-0.25 pts

A3.

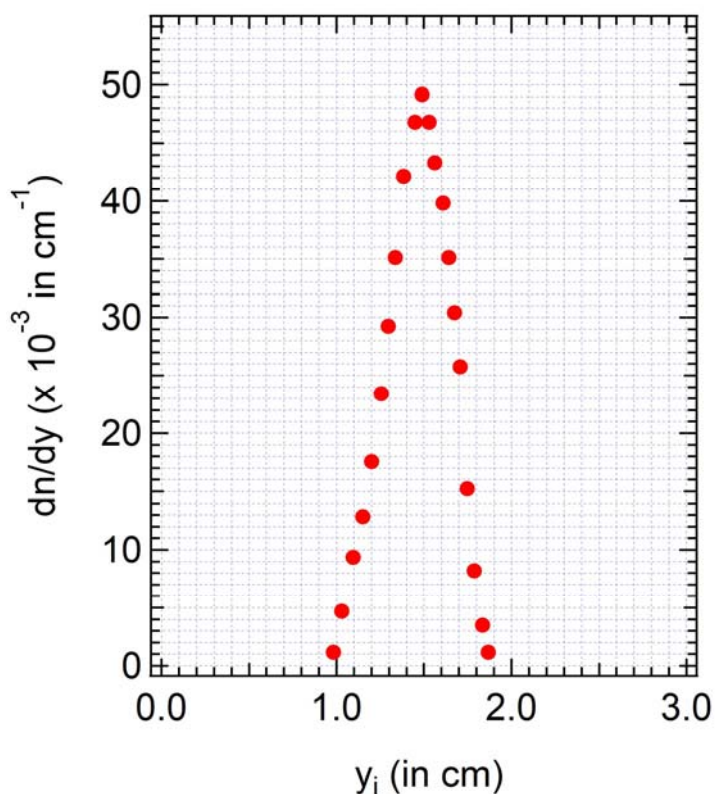
i	Y_i (cm)	dn/dY
1	1.86749	0.00117
2	1.83529	0.00351
3	1.78699	0.00819
4	1.74674	0.01521
5	1.70650	0.02574

Table 2 of

$C_0 = 33 \text{ g/150 mL}$.

data = 20

	<table> <tr><td>6</td><td>1.67430</td><td>0.03043</td></tr> <tr><td>7</td><td>1.64210</td><td>0.03511</td></tr> <tr><td>8</td><td>1.60990</td><td>0.03979</td></tr> <tr><td>9</td><td>1.56161</td><td>0.04330</td></tr> <tr><td>10</td><td>1.52941</td><td>0.04681</td></tr> <tr><td>11</td><td>1.48916</td><td>0.04915</td></tr> <tr><td>12</td><td>1.44891</td><td>0.04681</td></tr> <tr><td>13</td><td>1.38452</td><td>0.04213</td></tr> <tr><td>14</td><td>1.33622</td><td>0.03511</td></tr> <tr><td>15</td><td>1.29597</td><td>0.02926</td></tr> <tr><td>16</td><td>1.25572</td><td>0.02340</td></tr> <tr><td>17</td><td>1.19938</td><td>0.01755</td></tr> <tr><td>18</td><td>1.15108</td><td>0.01287</td></tr> <tr><td>19</td><td>1.09473</td><td>0.00936</td></tr> <tr><td>20</td><td>1.03034</td><td>0.00468</td></tr> <tr><td>21</td><td>0.98204</td><td>0.00117</td></tr> </table> 48TH IPHO 2017 YOGYAKARTA- INDONESIA 16 - 24 JULY 2017 Jury must check the data in table # wrong data point < 3 3<# wrong data point < 6 # wrong data point > 6	6	1.67430	0.03043	7	1.64210	0.03511	8	1.60990	0.03979	9	1.56161	0.04330	10	1.52941	0.04681	11	1.48916	0.04915	12	1.44891	0.04681	13	1.38452	0.04213	14	1.33622	0.03511	15	1.29597	0.02926	16	1.25572	0.02340	17	1.19938	0.01755	18	1.15108	0.01287	19	1.09473	0.00936	20	1.03034	0.00468	21	0.98204	0.00117	(0.25 pts) - 0 - 0.05 pts - 0.25pts
6	1.67430	0.03043																																																
7	1.64210	0.03511																																																
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A3.		Plot dn/dY vs Y $C_0 = 33 \text{ g/150 mL}$. (0.25 pts)																																																



without x-axis label

without x-axis unit

wrong x-axis unit

without y-axis label

without y-axis unit

wrong y-axis unit

Ordinate axis represented in 2 digid behind point

Ordinate axis represented in 3 digid behind point

Random shape of the curve

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.05 pts

-0 pts

-0.25 pts

A4.

(0.3 pts)

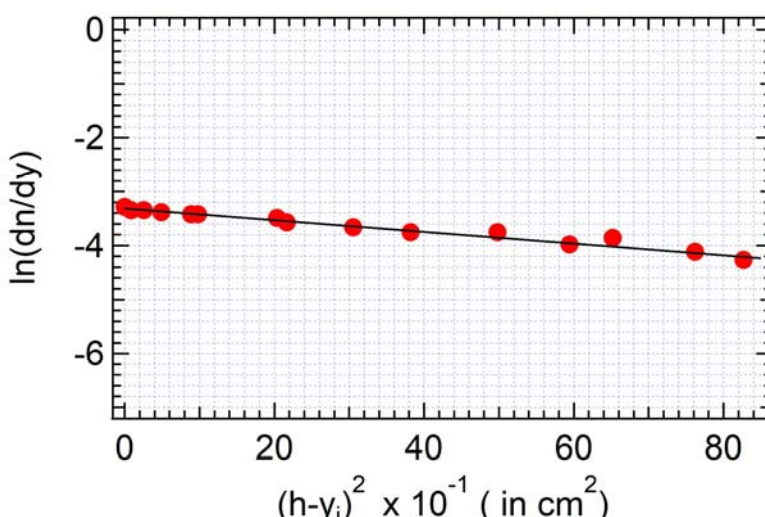
h for 23 g/ 150 mL = (1.5 ± 0.1) cm

0.1 pts

	h for 28 g/ 150 mL = (1.5 ± 0.1) cm	0.1 pts
	h for 33 g/ 150 mL = (1.5 ± 0.1) cm	0.1 pts
	If h is correctly determined from graph A3 for each concentration	- 0
	If h is not correctly determined from graph A3 for each concentration	-0.1

B : Determination of Diffusion Coefficient (4.2 points)

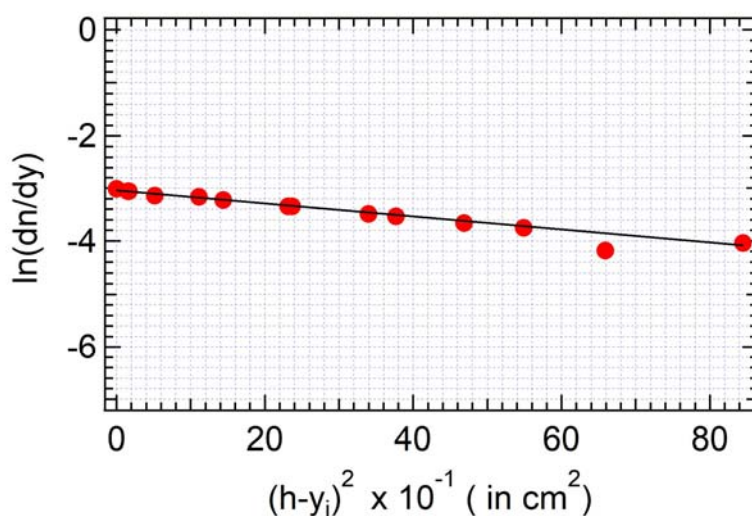
Question	Answer	Marks												
B1. (0.9 pts)	Linear form of eq.(3) $\ln\left(\frac{dn}{dy}\right) \approx m(h - Y)^2 + C \quad (b1)$ $m = -\frac{1}{4D_e t}$ Constant : $C = \ln\left(\left(\frac{dn}{dc}\right)\left(\frac{C_0}{2\sqrt{\pi D_e t}}\right)\right)$ Other than (b1)	0.9 pt -0.9 pts												
B2. (1.8 pts)	<table border="1"> <thead> <tr> <th>i</th><th>(h-y_i)²</th><th>ln(dn/dy)</th></tr> </thead> <tbody> <tr> <td>1</td><td>0.06592</td><td>-3.86003</td></tr> <tr> <td>2</td><td>0.050423</td><td>-3.75467</td></tr> <tr> <td>3</td><td>0.031065</td><td>-3.65936</td></tr> </tbody> </table>	i	(h-y _i) ²	ln(dn/dy)	1	0.06592	-3.86003	2	0.050423	-3.75467	3	0.031065	-3.65936	Table 3 of $C_0 = 23$ g /150 mL.
i	(h-y _i) ²	ln(dn/dy)												
1	0.06592	-3.86003												
2	0.050423	-3.75467												
3	0.031065	-3.65936												

	<table border="1"> <tr><td>4</td><td>0.020752</td><td>-3.4923</td></tr> <tr><td>5</td><td>0.00917</td><td>-3.41819</td></tr> <tr><td>6</td><td>0.005128</td><td>-3.3831</td></tr> <tr><td>7</td><td>0.000984</td><td>-3.3492</td></tr> <tr><td>8</td><td>6.99E-07</td><td>-3.28466</td></tr> <tr><td>9</td><td>0.002414</td><td>-3.3492</td></tr> <tr><td>10</td><td>0.009493</td><td>-3.41819</td></tr> <tr><td>11</td><td>0.021237</td><td>-3.57235</td></tr> <tr><td>12</td><td>0.037646</td><td>-3.75467</td></tr> <tr><td>13</td><td>0.05872</td><td>-3.97781</td></tr> </table> Jury must check the data in table # of data point > 10 3 ≤ # of data point < 10 # of data point < 3 # wrong data point < 3 3 < # wrong data point < 6 # wrong data point > 6	4	0.020752	-3.4923	5	0.00917	-3.41819	6	0.005128	-3.3831	7	0.000984	-3.3492	8	6.99E-07	-3.28466	9	0.002414	-3.3492	10	0.009493	-3.41819	11	0.021237	-3.57235	12	0.037646	-3.75467	13	0.05872	-3.97781	# data = 10 (0.3 pts) -0 pts -0.05 pts -0.3 pts - 0 - 0.05 pts - 0.25 pts
4	0.020752	-3.4923																														
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13	0.05872	-3.97781																														
B2	 Using linear regression of eq. (B1.1), we obtain m (slope) = -10 cm^{-2} till -8.8 cm^{-2}	Plot of Table 3 $C_0 = 23 \text{ g/150 mL}$ # data = 10 (0.3pts)																														

	without x-axis label without x-axis unit wrong x-axis unit without y-axis label without y-axis unit wrong y-axis unit # of data point in linear range > 10 3 ≤ # of data point in linear range < 10 # of data point in linear range < 3 or random shape of curve m is out of range	-0.01 pts -0.01 pts -0.01 pts -0.01 pts -0.01 pts -0.01 pts - 0 - 0.05 pts - 0.25 pts -0.3 pts																																										
B2.	<table border="1"> <thead> <tr> <th>i</th><th>(h-y_i)²</th><th>ln(dn/dy)</th></tr> </thead> <tbody> <tr><td>1</td><td>0.057912</td><td>-3.75467</td></tr> <tr><td>2</td><td>0.033968</td><td>-3.57235</td></tr> <tr><td>3</td><td>0.023136</td><td>-3.41819</td></tr> <tr><td>4</td><td>0.014378</td><td>-3.3492</td></tr> <tr><td>5</td><td>0.007693</td><td>-3.28466</td></tr> <tr><td>6</td><td>0.001553</td><td>-3.22404</td></tr> <tr><td>7</td><td>6.99E-07</td><td>-3.19505</td></tr> <tr><td>8</td><td>0.002414</td><td>-3.22404</td></tr> <tr><td>9</td><td>0.007989</td><td>-3.25389</td></tr> <tr><td>10</td><td>0.018955</td><td>-3.3492</td></tr> <tr><td>11</td><td>0.037646</td><td>-3.53152</td></tr> <tr><td>12</td><td>0.071007</td><td>-3.86003</td></tr> <tr><td>13</td><td>0.099079</td><td>-4.26549</td></tr> </tbody> </table> Jury must check the data in table	i	(h-y _i) ²	ln(dn/dy)	1	0.057912	-3.75467	2	0.033968	-3.57235	3	0.023136	-3.41819	4	0.014378	-3.3492	5	0.007693	-3.28466	6	0.001553	-3.22404	7	6.99E-07	-3.19505	8	0.002414	-3.22404	9	0.007989	-3.25389	10	0.018955	-3.3492	11	0.037646	-3.53152	12	0.071007	-3.86003	13	0.099079	-4.26549	Table 3 of C₀ = 28 g /150 mL # data = 10 (0.3 pts)
i	(h-y _i) ²	ln(dn/dy)																																										
1	0.057912	-3.75467																																										
2	0.033968	-3.57235																																										
3	0.023136	-3.41819																																										
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[illegible]

	# of data point in linear range > 10 3 ≤ # of data point in linear range < 10 # of data point in linear range < 3 or random shape of curve m is out of range	-0.05 pts -0.3 pts -0.3 pts																																										
B2.	<table border="1"> <thead> <tr> <th>i</th><th>(h-y_i)²</th><th>ln(dn/dy)</th></tr> </thead> <tbody> <tr><td>1</td><td>0.046873</td><td>-3.65936</td></tr> <tr><td>2</td><td>0.033968</td><td>-3.4923</td></tr> <tr><td>3</td><td>0.023136</td><td>-3.3492</td></tr> <tr><td>4</td><td>0.014378</td><td>-3.22404</td></tr> <tr><td>5</td><td>0.005128</td><td>-3.13948</td></tr> <tr><td>6</td><td>0.001553</td><td>-3.06152</td></tr> <tr><td>7</td><td>6.99E-07</td><td>-3.01273</td></tr> <tr><td>8</td><td>0.001688</td><td>-3.06152</td></tr> <tr><td>9</td><td>0.011126</td><td>-3.16688</td></tr> <tr><td>10</td><td>0.023647</td><td>-3.3492</td></tr> <tr><td>11</td><td>0.037646</td><td>-3.53152</td></tr> <tr><td>12</td><td>0.054884</td><td>-3.75467</td></tr> <tr><td>13</td><td>0.08446</td><td>-4.04235</td></tr> </tbody> </table> Jury must check the data in table # of data point > 10 3 ≤ # of data point < 10 # of data point < 3 # wrong data point < 3 3 < # wrong data point < 6 # wrong data point > 6	i	(h-y _i) ²	ln(dn/dy)	1	0.046873	-3.65936	2	0.033968	-3.4923	3	0.023136	-3.3492	4	0.014378	-3.22404	5	0.005128	-3.13948	6	0.001553	-3.06152	7	6.99E-07	-3.01273	8	0.001688	-3.06152	9	0.011126	-3.16688	10	0.023647	-3.3492	11	0.037646	-3.53152	12	0.054884	-3.75467	13	0.08446	-4.04235	Table 3 of C₀ = 33 g /150 mL # data = 10 (0.3 pts) -0 pts -0.05 pts -0.3 pts - 0 - 0.05 pts - 0.25
i	(h-y _i) ²	ln(dn/dy)																																										
1	0.046873	-3.65936																																										
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B2.		Plot of Table 3 C₀ = 33 g/150 mL																																										



data =
10

(0.3pts)

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.01 pts

-0.3 pts

-0 pts

-0.05 pts

-0.3

Using linear regression of eq. (B1.1), we obtain

m (slope) = -11.3 cm^{-2} till -12.8 cm^{-2}

without x-axis label

without x-axis unit

wrong x-axis unit

without y-axis label

without y-axis unit

wrong y-axis unit

m is out of range

of data point in linear range > 10

$3 \leq$ # of data point in linear range < 10

of data point in linear range < 3 or random shape of curve

B3

(1.5 pts)

D of 23 g/ 150 mL = $(1.38 \text{ till } 1.58) \times 10^{-5} \text{ cm}^2/\text{s}$

0.5 pts

D of 28 g/ 150 mL = $(1.26 \text{ till } 1.46) \times 10^{-5} \text{ cm}^2/\text{s}$

0.5 pts

	D of 33 g/ 150 mL = $(1.03 \text{ till } 1.23) \times 10^{-5} \text{ cm}^2/\text{s}$ D is out of range for each concentration	0.5 pts- -0.5 pts
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C. Nonlinear diffusion (1.3 points)

Question	Answer	Marks
C1. (1.3 pts)	Without error bars Value of C not stated in $C_0/2$	Plot D vs. C_0 0.8 pts -0 -0.4 pts
C1.	$\frac{d}{dc} D = -4.2 \times 10^{-5} \text{ cm}^2 \text{ mL } g^{-1} s^{-1} \text{ till}$ $-15.8 \times 10^{-5} \text{ cm}^2 \text{ mL } g^{-1} s^{-1}$	0.5 pts -0.01 pts -0.5 pts



E1. Marking Scheme & Solution

Student Code

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Experimental
Question

1

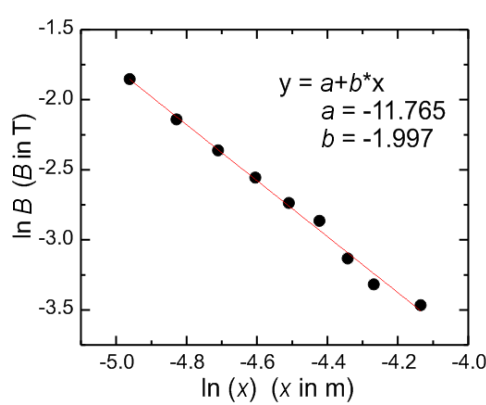
page 19 of 19



Parallel Dipole Line Magnetic Trap for Earthquake & Volcanic Sensing (10 points)

A. BASIC CHARACTERISTICS OF PDL TRAP

1. Determination of the magnet's magnetization (M) (2.5 pts)

Question	Answer	Marks																																																												
A.1 0.1 pts	Record zero offset (B_0) of the Teslameter without any magnet nearby. Subtract subsequent field measurement with this value Example from a Teslameter unit: $B_0 = 0.86 \text{ mT}$	0.08 pts range (-10 mT to 10 mT) Correct unit: 0.02 pts																																																												
A.2 1.15 pts	Measure magnetic field B vs. x in the near field region ($7 \leq x \leq 16 \text{ mm}$). <u>Where x is the position measured from the center of the magnet.</u> Record and plot your result on the answer sheet. $x_0 = 4 \text{ mm}$, $B_0=0.86 \text{ mT}$. Δx is measured from surface. $B = B_{\text{raw}} - B_0$ <table><tr><th>Δx (mm)</th><th>X (mm)</th><th>B_{raw} (T)</th><th>B (T)</th><th>$\ln(x)$ x in m</th><th>$\ln(B)$ B in T</th></tr><tr><td>3</td><td>7</td><td>0.1576</td><td>0.1567</td><td>-4.962</td><td>-1.853</td></tr><tr><td>4</td><td>8</td><td>0.1186</td><td>0.1177</td><td>-4.828</td><td>-2.139</td></tr><tr><td>5</td><td>9</td><td>0.0951</td><td>0.0942</td><td>-4.710</td><td>-2.362</td></tr><tr><td>6</td><td>10</td><td>0.0785</td><td>0.0776</td><td>-4.605</td><td>-2.556</td></tr><tr><td>7</td><td>11</td><td>0.0657</td><td>0.0648</td><td>-4.510</td><td>-2.736</td></tr><tr><td>8</td><td>12</td><td>0.0579</td><td>0.0570</td><td>-4.423</td><td>-2.864</td></tr><tr><td>9</td><td>13</td><td>0.0445</td><td>0.0436</td><td>-4.343</td><td>-3.132</td></tr><tr><td>10</td><td>14</td><td>0.0371</td><td>0.0362</td><td>-4.269</td><td>-3.318</td></tr><tr><td>12</td><td>16</td><td>0.0321</td><td>0.0312</td><td>-4.135</td><td>-3.466</td></tr></table> Plot: 	Δx (mm)	X (mm)	B_{raw} (T)	B (T)	$\ln(x)$ x in m	$\ln(B)$ B in T	3	7	0.1576	0.1567	-4.962	-1.853	4	8	0.1186	0.1177	-4.828	-2.139	5	9	0.0951	0.0942	-4.710	-2.362	6	10	0.0785	0.0776	-4.605	-2.556	7	11	0.0657	0.0648	-4.510	-2.736	8	12	0.0579	0.0570	-4.423	-2.864	9	13	0.0445	0.0436	-4.343	-3.132	10	14	0.0371	0.0362	-4.269	-3.318	12	16	0.0321	0.0312	-4.135	-3.466	Correct label and unit for data: 0.1 pts Number of correct data for $x \leq 16 \text{ mm}$: 0.05 pts for each correct data, max 0.45 pts Plot: -Correct axis label and unit: 0.05 pts - Using around 75% of plot area: 0.05 pts -For each correct data point: 0.05 pts, max. 0.4 pts -Adding trendline: 0.1 pts
Δx (mm)	X (mm)	B_{raw} (T)	B (T)	$\ln(x)$ x in m	$\ln(B)$ B in T																																																									
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A.3 0.75 pts	Use your experimental data to determine the value of the exponent p. Linear regression (LR) $y = a + b x : B = \frac{\mu_0 m}{2\pi L} \frac{1}{x^p}$ $\ln(B) = a - p \ln x$ where $a = \ln\left(\frac{\mu_0 m}{2\pi L}\right)$. LR yields : $a = -11.765$ and $b = -1.997$ The power exponent: $p = -b = 2.0$ Note that this is in very good agreement with the exact result: at short distance ($x < L$) a diametric (or a dipole line) magnet has $B \sim 1/r^2$ dependence. See Ref. [1] , Fig. 2c.	Obtaining p from graph: 0.05 pts Obtaining p from linear regression: 0.1 pts Result: $p = 1.8 - 2.2 : 0.65$ pts $p = 1.6 - 2.4 : 0.35$ pts Result with wrong sign: $p = (-1.8) - (-2.2) : 0.4$pts $p = (-1.6) - (-2.4) : 0.1$pts More than two sig. figs.: minus 0.05 pts
A.4 0.5 pts	Determine the magnet's magnetization M. $m = \frac{2\pi L}{\mu_0} \exp(a) = 0.987 \text{ Am}^2$ $M = \frac{m}{\pi R^2 L} = 1.2 \times 10^6 \text{ A/m}$ This is close to the more accurate results from more extensive measurements to far field (see Ref. [1], Fig. 2c) and we use this value for subsequent questions: $M = 1.1 \times 10^6 \text{ A/m}$	Correct unit: 0.05 pts Obtaining intercept (a) from graph: 0.025 pts Obtaining intercept from LR: 0.05 pts Correct formula for m and/or M : 0.1 pts Result for M ($\times 10^6 \text{ A/m}$): $0.9 - 1.4 : 0.3$ pts $0.1 - 2.5 : 0.15$ pts More than 2 sig. figs.: minus 0.05 pts

2. The Magnetic Levitation Effect and Magnetic Susceptibility (χ) (1 pts)

Question	Answer	Marks
A.5 0.1 pts	Place gently a graphite rod HB/0.5 and length = 8 mm. Measure the levitation height y_0 of the rod (see Fig. 7a). Hint: Use the insert ruler provided as shown in Fig. 7b. Press the ruler on the magnets to read the position of the graphite rod We levitate graphite HB/0.5, $l = 8 \text{ mm}$. Using the insert-ruler, we measure approximately $\Delta y = 1 \text{ mm}$ from the top of the magnet surface. Thus: $y_0 = R - \Delta y = (3.2 - 1) \text{ mm} = 2.2 \text{ mm}$	correct unit: 0.02 $y_0 = (1.7 - 2.2) \text{ mm} : 0.08$ pts partial credit: Only $\Delta y = (1 - 1.5) \text{ mm} : 0.03$ pts

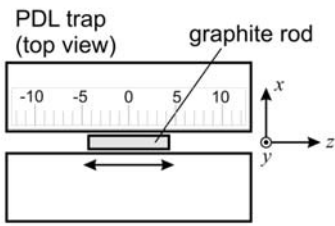
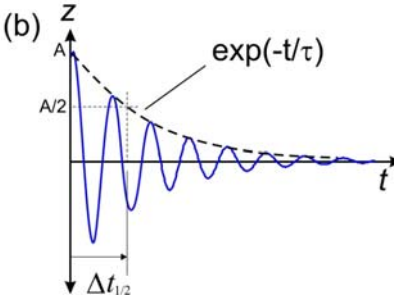
A.6 0.8 pts	Use the result from part A.5 to determine the magnetic susceptibility χ of the graphite rod. Solving for χ: $mg = F_y = -\frac{\mu_0 M^2 \chi V_R}{2} \frac{R^4}{a^5} f_Y(y_0/a)$ $\chi = -\frac{2\rho g a^5}{\mu_0 M^2 R^4 f_Y(y_0/a)}$ We calculate: $a = R + g_M / 2 = (3.2 + 1.5/2) \text{ mm} = 3.95 \text{ mm}$. Using $y_0 = 2.2 \text{ mm}$: $f_Y(u) = \frac{4u(3-u^2)(1-u^2)}{(1+u^2)^5}$, $f_Y(y_0/a) = f_Y(2.2/3.95) = 1.07$ Using the correct $M = 1.1 \times 10^6 \text{ A/m}$; and $R = 3.2 \text{ mm}$, $\rho = 1680 \text{ kg/m}^3$ we have: $\chi = -1.85 \times 10^{-4}$. Note that this is very good agreement with the literature value for graphite pencil lead: $\chi = -2 \times 10^{-4}$ (see Ref.[1], pg. 2 & Ref.[2]). The sign is negative indicating a diamagnetic material.	Correct expression for χ: 0.4 pts Result for χ ($\times 10^{-4}$) -(1.4 to 2.6) : 0.4 pts -(0.5 to 4) : 0.2 pts Wrong sign: minus 0.1 pts
A.7 0.1 pts	What kind of magnetic material is graphite? Choose one: (i) Ferromagnetic; (ii) Paramagnetic; or (iii) Diamagnetic? (iii) Diamagnetic. Because: (1) Graphite is repelled by magnetic field (2) The sign of χ is negative.	Correct choice: 0.1 pts

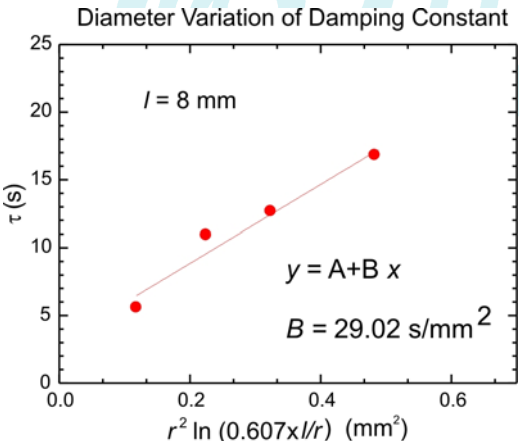
3. The camelback potential oscillation and magnetic susceptibility (χ) (1 points)

Question	Answer	Marks																		
A.8 0.2 pts	<u>Perform an oscillation for the "HB/0.5" graphite and $l=8$ mm. Limit to small oscillation amplitude i.e. $A < 4$mm.</u> <u>Determine the oscillation period. (The oscillation will decay over time due to damping, ignore this damping effect).</u> Example, we measured 5 oscillations of HB/0.5 with length $l = 8$ mm. We displaced it by ~ 3 mm and let it oscillates. We measured 5 oscillation periods: <table><tr><th>Trial</th><th>5 T_z</th><th></th><th></th><th></th><th></th></tr><tr><td></td><td>(s)</td><td></td><td></td><td></td><td></td></tr><tr><td>1</td><td>6.12</td><td></td><td></td><td></td><td></td></tr></table>	Trial	5 T_z						(s)					1	6.12					Correct label and unit: 0.02 pts Number of correct data each 0.01 pts, max 0.03 pts Number of oscillation < 3 : 0 pts >= 3 : 0.05 pts $T_z = (1.2 - 1.5)$ s: 0.1 pts
Trial	5 T_z																			
	(s)																			
1	6.12																			

	<table> <tr> <td>2</td> <td>6.13</td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td>3</td> <td>6.14</td> <td></td> <td></td> <td></td> <td></td> </tr> </table> Average : $T_z = 1.23$ s	2	6.13					3	6.14					
2	6.13													
3	6.14													
A.9 0.8 pts	<i>Calculate the magnetic susceptibility (χ) of the graphite using this oscillation</i> For harmonic oscillator : $k_z = m_R \omega^2$, solving for χ: $\chi = -\frac{k_z}{C_1 \mu_0 M^2 V_r} = \frac{\omega^2 \rho}{C_1 \mu_0 M^2}$ Using the correct $M = 1.1 \times 10^6$ A/m. Using $C_1 = 198.6/\text{m}^2$, and $T_z = 1.23$ s, we obtain $\chi = -1.5 \times 10^{-4}$. Note that this is in good agreement with the literature value of the graphite pencil lead: $\chi = -2 \times 10^{-4}$ (Ref.[1], pg. 2); and the sign is negative indicating a diamagnetic material.	Correct expression for χ: 0.4 pts Result for χ ($\times 10^{-4}$) -(1.4 to 2.6) : 0.4 pts -(0.5 to 4) : 0.2 pts Wrong sign: minus 0.1 pts												

4. Oscillator quality factor (Q) and estimate of air viscosity μ_A (3.0 points)

Question	Answer	Marks
A.10 0.5 pts	We need to determine the damping time constant of the oscillation τ. Sketch how you measure τ in a simple way. (a)  (b)  The trick is to use "half-time" concept of exponential decay. We set the oscillation and measure the time taken for the amplitude to halve. The lifetime is: $\tau = \frac{\Delta t_{1/2}}{\ln 2}$	Correct idea: 0.3 pts Correct expression for τ: 0.2 pts
A.11 1.5 pts	Perform oscillation damping experiments with a group of rods with various diameters and fixed length of 8 mm. Determine the damping time constant τ for each rods	Correct label and unit 0.1 Number of correct data

	We displaced the graphite by ~4 mm, started the stopwatch and then waited until it decays to half. <table><tr><th>Trial</th><th>Diam.</th><th>Actual Radius</th><th>$\Delta t_{1/2}$</th><th>Mean $\Delta t_{1/2}$</th><th>τ</th><th>$r^2 \times \ln(0.607 l/r)$</th></tr><tr><td></td><td>(mm)</td><td>(mm)</td><td>(s)</td><td>(s)</td><td>(s)</td><td>(mm²)</td></tr><tr><td>1</td><td>0.3</td><td>0.19</td><td>3.89</td><td>3.913</td><td>5.646</td><td>0.117</td></tr><tr><td></td><td></td><td></td><td>3.97</td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td>3.88</td><td></td><td></td><td></td></tr><tr><td>2</td><td>0.5</td><td>0.28</td><td>7.69</td><td>7.617</td><td>10.989</td><td>0.224</td></tr><tr><td></td><td></td><td></td><td>7.57</td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td>7.59</td><td></td><td></td><td></td></tr><tr><td>3</td><td>0.7</td><td>0.35</td><td>8.77</td><td>8.82</td><td>12.73</td><td>0.322</td></tr><tr><td></td><td></td><td></td><td>8.81</td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td>8.88</td><td></td><td></td><td></td></tr><tr><td>4</td><td>0.9</td><td>0.45</td><td>12.4</td><td>11.70</td><td>16.88</td><td>0.482</td></tr><tr><td></td><td></td><td></td><td>11.33</td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td>11.38</td><td></td><td></td><td></td></tr></table>	Trial	Diam.	Actual Radius	$\Delta t_{1/2}$	Mean $\Delta t_{1/2}$	τ	$r^2 \times \ln(0.607 l/r)$		(mm)	(mm)	(s)	(s)	(s)	(mm ²)	1	0.3	0.19	3.89	3.913	5.646	0.117				3.97							3.88				2	0.5	0.28	7.69	7.617	10.989	0.224				7.57							7.59				3	0.7	0.35	8.77	8.82	12.73	0.322				8.81							8.88				4	0.9	0.45	12.4	11.70	16.88	0.482				11.33							11.38				for each diameter (4): < 3 : 0.1 pts >=3 : 0.25 pts (max 1.0 pts) Positive monotonic trend for τ vs. diameter from 0.3 to 0.9 mm with $\tau = 5$ to 20 sec : 0.4 pts
Trial	Diam.	Actual Radius	$\Delta t_{1/2}$	Mean $\Delta t_{1/2}$	τ	$r^2 \times \ln(0.607 l/r)$																																																																																														
	(mm)	(mm)	(s)	(s)	(s)	(mm ²)																																																																																														
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A.12 1 pts	Determine the air viscosity μ_A Diameter Variation of Damping Constant  We have: $\tau = b r^2 \ln \left(0.607 \times \frac{l}{r} \right)$, where: $b = \frac{2}{3} \frac{\rho}{\mu_A}$. We performed linear regression $y = a + b x$, with $y = \tau$ and $x = r^2 \ln \left(0.607 \times \frac{l}{r} \right)$. We obtain: $b = 29.02 \text{ s/mm}^2$. $\mu_A = \frac{2}{3} \frac{\rho}{b} = 38.6 \cdot 10^{-6} \text{ Pa.s} \quad (1 \text{ Pa.s} = 1 \text{ kg /m s})$ Note that this is about 2.1x the actual viscosity of air of 18.2μ.Pa.s. The discrepancy is due to the ellipsoidal	Correct unit: 0.05 Obtaining result with linear regression or plot: 0.25 pts Result μ_A ($\times 10^{-6}$ Pa.s): 20 - 60 : 0.7 pts 10 - 80 : 0.4 pts 1 - 100 : 0.1 pts																																																																																																		

	approximation of the Stokes drag (vs. the actual cylindrical shape of the rod) and the proximity effect of the rod to the magnet (wall effect). Another factor is the crude nature of our manual τ determination. See Ref. [1], pg. 8.	
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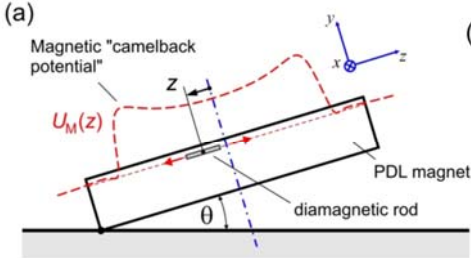
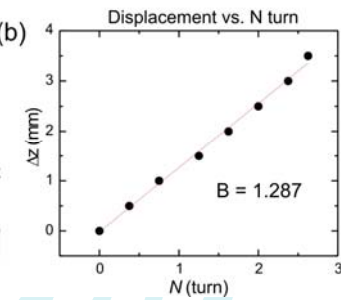
B. SENSOR APPLICATION OF THE PDL TRAP

5. PDL Trap Seismometer (0.5 pts)

Question	Answer	Marks
B.1 0.2 pts	<i>Which diameter of rod do you choose?</i> To obtain the lowest acceleration noise floor " a_n " we should choose the largest diameter graphite i.e. 0.9 mm, because their damping time is the longest and the mass is the largest.	Correct answer: 0.2 pts
B.2 0.3 pts	<i>Calculate the seismometer acceleration noise floor (a_n) for the rod of your choice!</i> For HB/0.9 and length $l = 8$ mm: We use $\tau = 16.9$ s; and $T = 298$ K, we have: $m_R = \rho \pi r^2 l = 8.55 \times 10^{-6}$ kg : $a_n = \sqrt{\frac{4k_B T \omega_0}{Q m_R}} = \sqrt{\frac{8k_B T}{\tau m_R}} = 1.5 \times 10^{-8} \text{ m}/(\text{s}^2 \text{ Hz}^{0.5})$	Correct unit: 0.1 Correct answer: 0.2 pts

6. PDL Trap Tiltmeter (2 pts)

Question	Answer	Marks
B.3 0.5 pts	<i>Derive the relation theoretically between displacement Δz with the screw thread size S and the number of turns (N).</i> $k_z \Delta z = m g \sin \theta = m g N S / D \quad \Delta z = \frac{m g S N}{k_z D}$ From Question 3, we also have $k_z = m \omega^2$: $\Delta z = \frac{g S}{\omega^2 D} N$	Correct expression: 0.5 pts Partial credit $k_z \Delta z = m g \sin \theta : 0.2$
B.4 1.25 pts	<i>By turning the screw slowly, determine the rod displacement Δz vs. the number of screw turns (N). Determine the thread size S</i>	Correct label and unit: 0.1 pts

	We measured the distance between screws: $D = 22$ cm, and we used the period from Q3: $T_z = 1.23$ s <table><tr><th>Δz (mm)</th><th>ϕ</th><th>N (turn)</th><th></th><th></th><th></th></tr><tr><td>0</td><td>0</td><td>0</td><td></td><td></td><td></td></tr><tr><td>0.5</td><td>135</td><td>0.375</td><td></td><td></td><td></td></tr><tr><td>1</td><td>270</td><td>0.75</td><td></td><td></td><td></td></tr><tr><td>1.5</td><td>450</td><td>1.25</td><td></td><td></td><td></td></tr><tr><td>2</td><td>585</td><td>1.625</td><td></td><td></td><td></td></tr><tr><td>2.5</td><td>720</td><td>2.0</td><td></td><td></td><td></td></tr><tr><td>3</td><td>855</td><td>2.375</td><td></td><td></td><td></td></tr><tr><td>3.5</td><td>945</td><td>2.625</td><td></td><td></td><td></td></tr></table> (a)  (b)  By performing linear regression: $y = a + b x$ We have $b = 1.287$ mm/turns : $S = \frac{b \omega^2 D}{g} = 0.75$ mm/turn. This is reasonably close to the actual value of the thread size: $S = (0.8 \pm 0.1)$ mm/turn.	Δz (mm)	ϕ	N (turn)				0	0	0				0.5	135	0.375				1	270	0.75				1.5	450	1.25				2	585	1.625				2.5	720	2.0				3	855	2.375				3.5	945	2.625				Distance between screws: $22.8 < D < 22.2$ cm : 0.1 pts Number of correct data: < 3 sets : 0 pts 3-5 sets: 0.15 pts >5 sets : 0.25 pts Obtaining result with linear regression or plot: 0.2 pts Result: $0.7 < S < 0.9$: 0.55 pts $0.5 < S < 1.1$: 0.15 pts Correct unit for S : 0.05
Δz (mm)	ϕ	N (turn)																																																						
0	0	0																																																						
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3.5	945	2.625																																																						
B.5 0.25 pts	When the ground tilt changes we want the graphite rod to go to equilibrium as fast as possible (instead of sustaining very long oscillation) to allow easy reading. What is the ideal Q factor for a tiltmeter? We need critical damping thus: $Q = 0.5$	Correct Q : 0.25 pts																																																						

REFERENCES:

- [1] Gunawan, O. & Virgus, Y. *The one-dimensional camelback potential in the parallel dipole line trap: Stability conditions and finite size effect.* J. Appl. Phys. 121, 133902, (2017). DOI:10.1063/1.4978876.
- [2] Gunawan, O., Virgus, Y. & Fai Tai, K. *A parallel dipole line system.* Appl. Phys. Lett. 106, 062407, (2015). DOI: 10.1063/1.4907931.